

New Approaches to Small-Scale Lensing of the Cosmic Microwave Background (CMB)

BORYANA HADZHIYSKA (HARVARD, CAMBRIDGE)

BLAKE SHERWIN (CAMBRIDGE)

MATHEW MADHAVACHERIL (PRINCETON)

SIMONE FERRARO (BERKELEY)

9 MARCH 2021

CMB-S4 meeting

Outline

1. Motivation

2. Lensing reconstruction methods

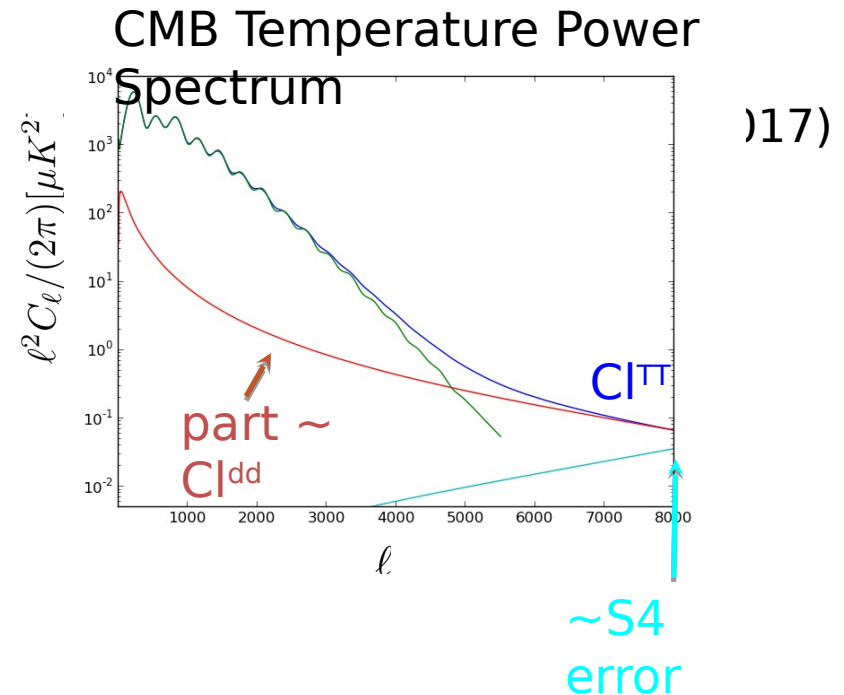
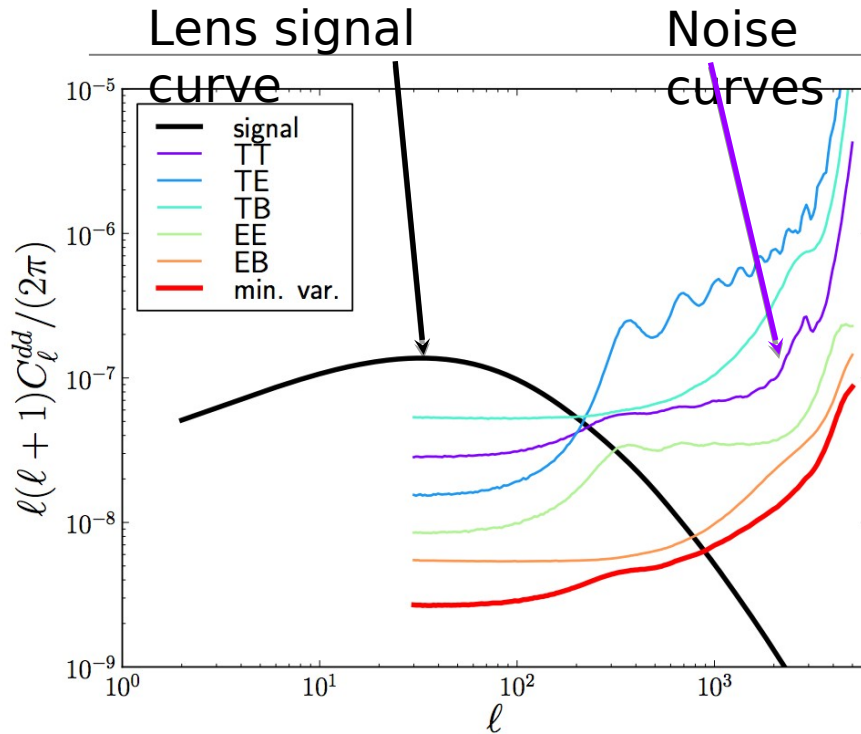
- a. Quadratic estimator (QE)

- b. Gradient-inversion (GI)

3. Caveats and next steps

4. Summary

Small-scale puzzle



- A puzzle: quadratic estimator noise gets large – seemingly cannot probe tiny CMB lenses / scales

- But with low enough noise, can read off tiny lenses from small-scale power spectrum.

Why go to small scales?

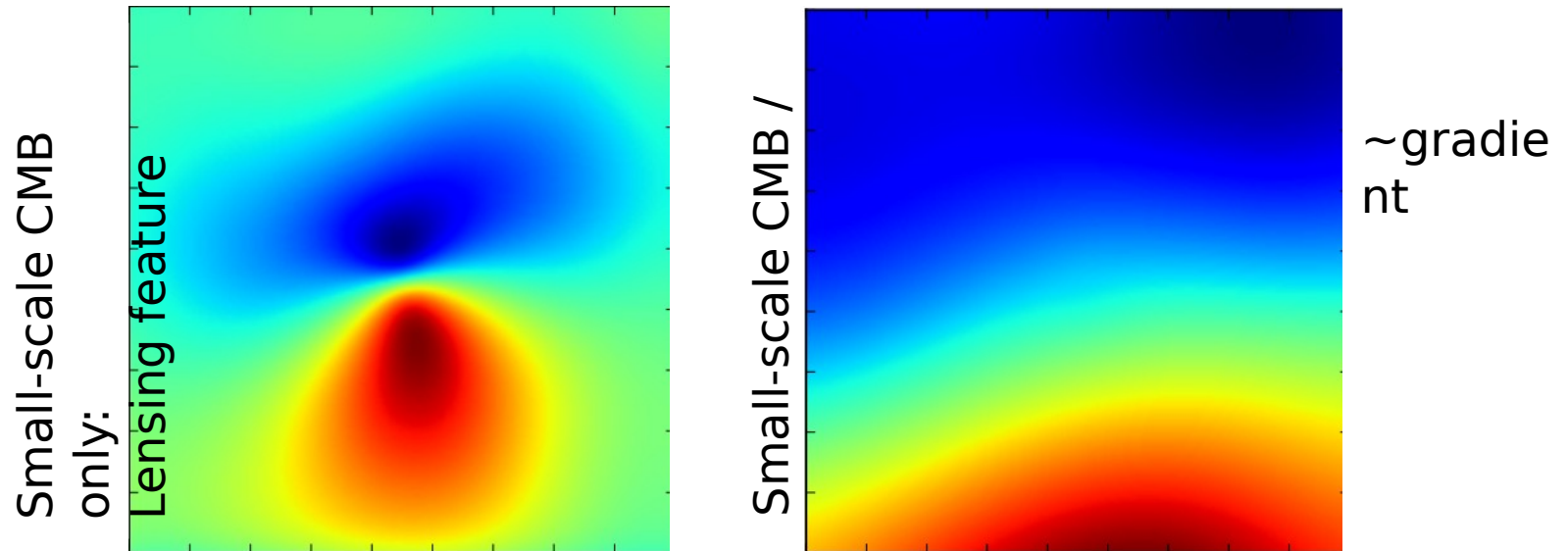
- Dark matter models (axions, warm dark matter, fuzzy dark matter)
- Cross-correlations with galaxy surveys (DESI, eBOSS, *Euclid*)
- Modeling of the one-halo term (assembly bias, baryonic physics, galaxy formation)

Will have measurements from ultra-deep survey LAT that we need to take full advantage of!

Outline

1. Motivation
- 2. Lensing reconstruction methods**
 - a. Quadratic estimator (QE)
 - b. Gradient-inversion (GI)
3. Caveats and next steps
4. Summary

Gradient Inversion Lensing Estimation

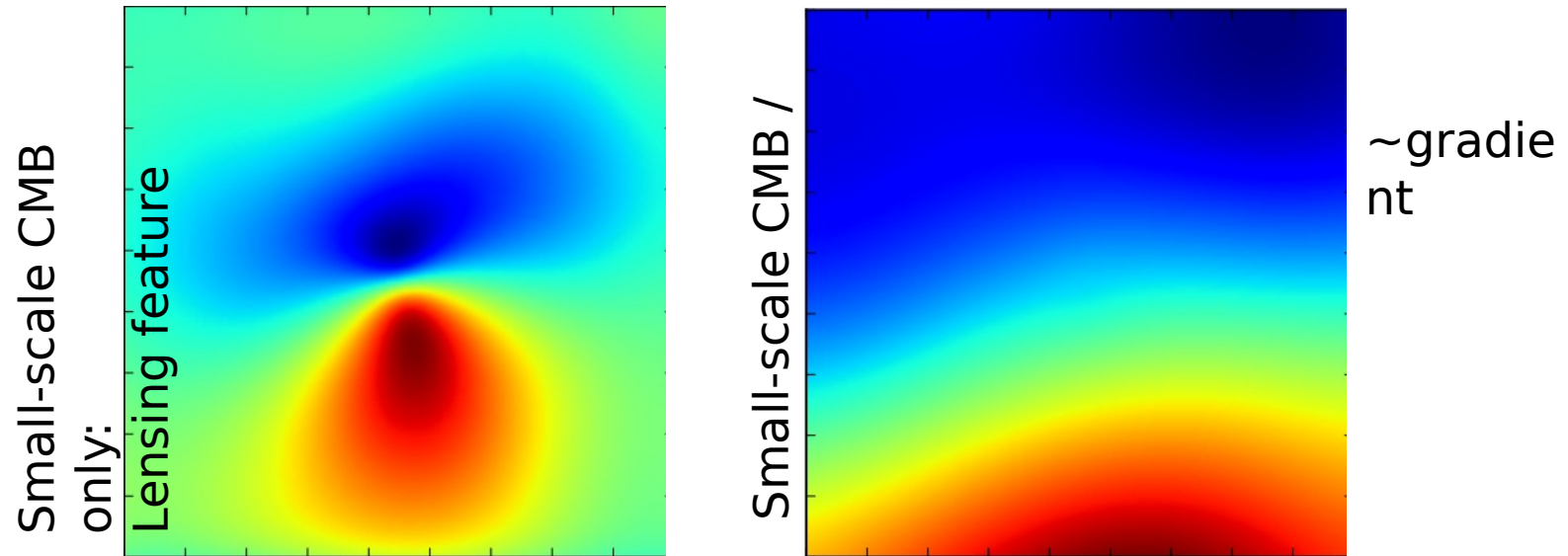


- On small scales, CMB gradient is effectively constant. Lensing expansion:

$$T(\mathbf{x}) = T^u(\mathbf{x} + \mathbf{d}) \approx T^u(\mathbf{x}) + \mathbf{d}(\mathbf{x}) \cdot \nabla T^u + \dots$$

Noise
Foreground
S

Gradient Inversion Lensing Estimation



- Suggests simple “gradient inversion” estimator:

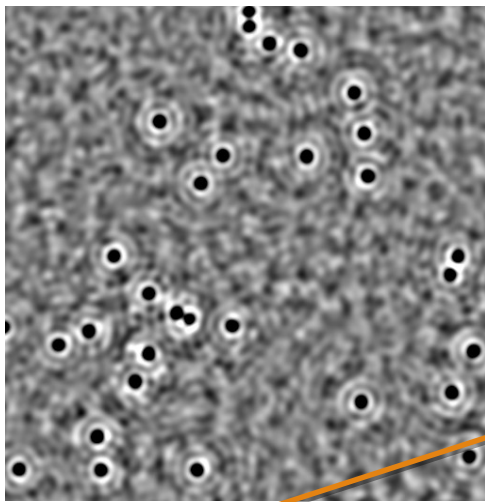
$$\hat{d}^{GI}(\mathbf{L}) = \frac{T(\mathbf{L})}{\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u} \quad \leftarrow \text{Not limited by cosmic variance; SNR} \sim \text{local gradient}$$

- Quadratic estimator: divides out $\langle \text{grad}^2 \rangle$ - extra error!

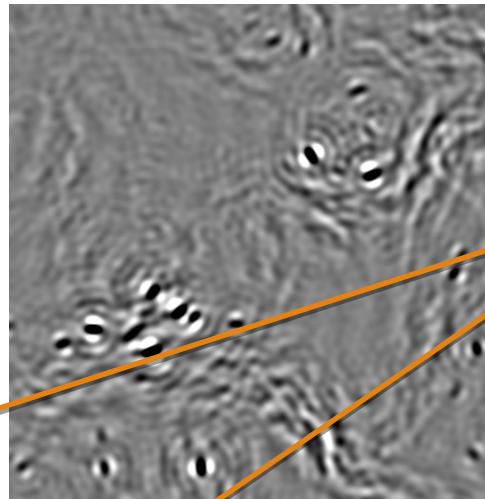
$$\hat{d}^{QE}(\mathbf{L}) = \hat{d}^{GI}(\mathbf{L}) \frac{(\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u)^2}{\langle (\hat{\mathbf{n}}_{\mathbf{L}} \cdot \nabla T^u)^2 \rangle}$$

Simulation: GI Lensing Maps and Spectra

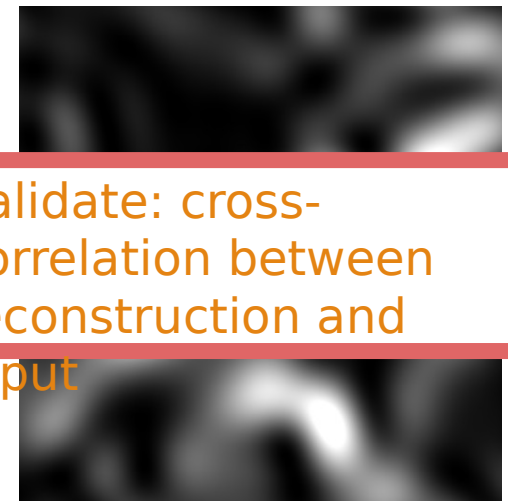
Expected noise is gradient-magnitude-dependent



True small-scale lens
map



GI
reconstruction



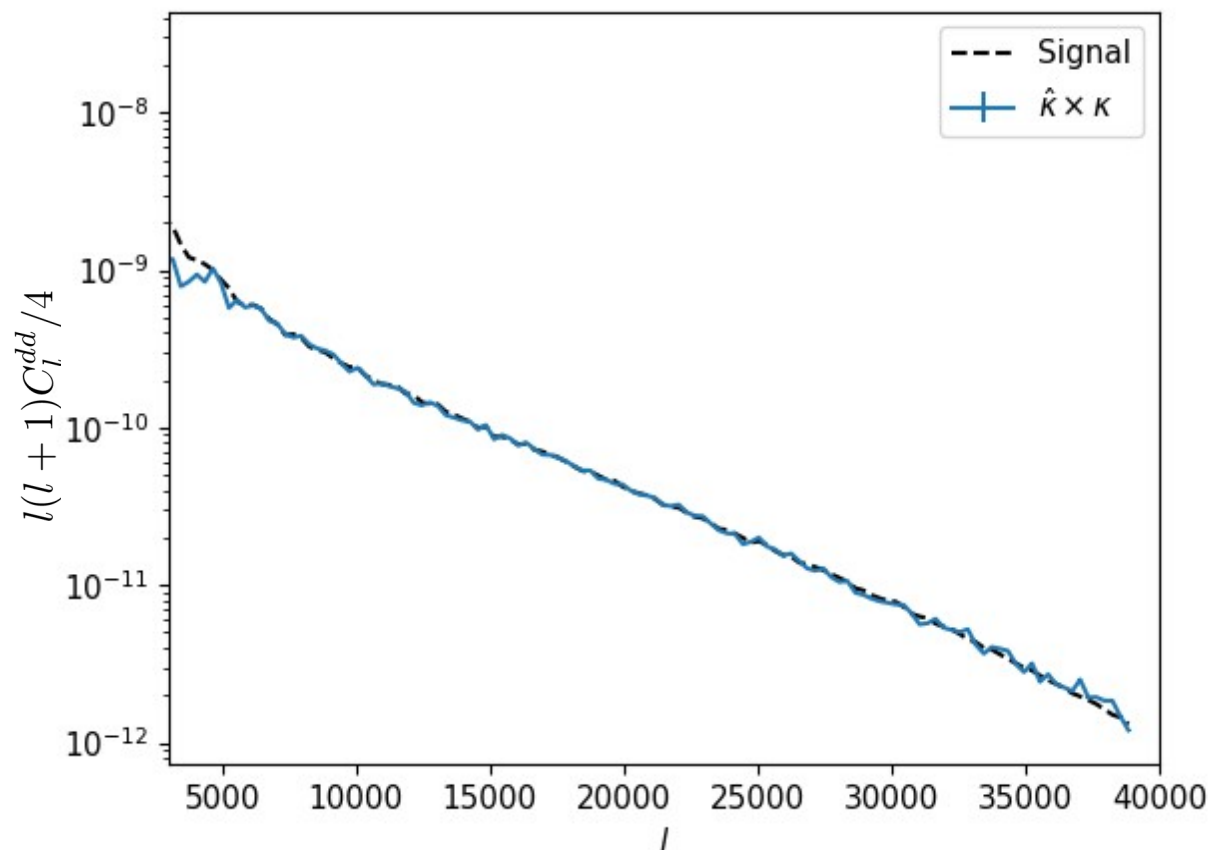
Gradient
magnitude

Validate: cross-correlation between reconstruction and input

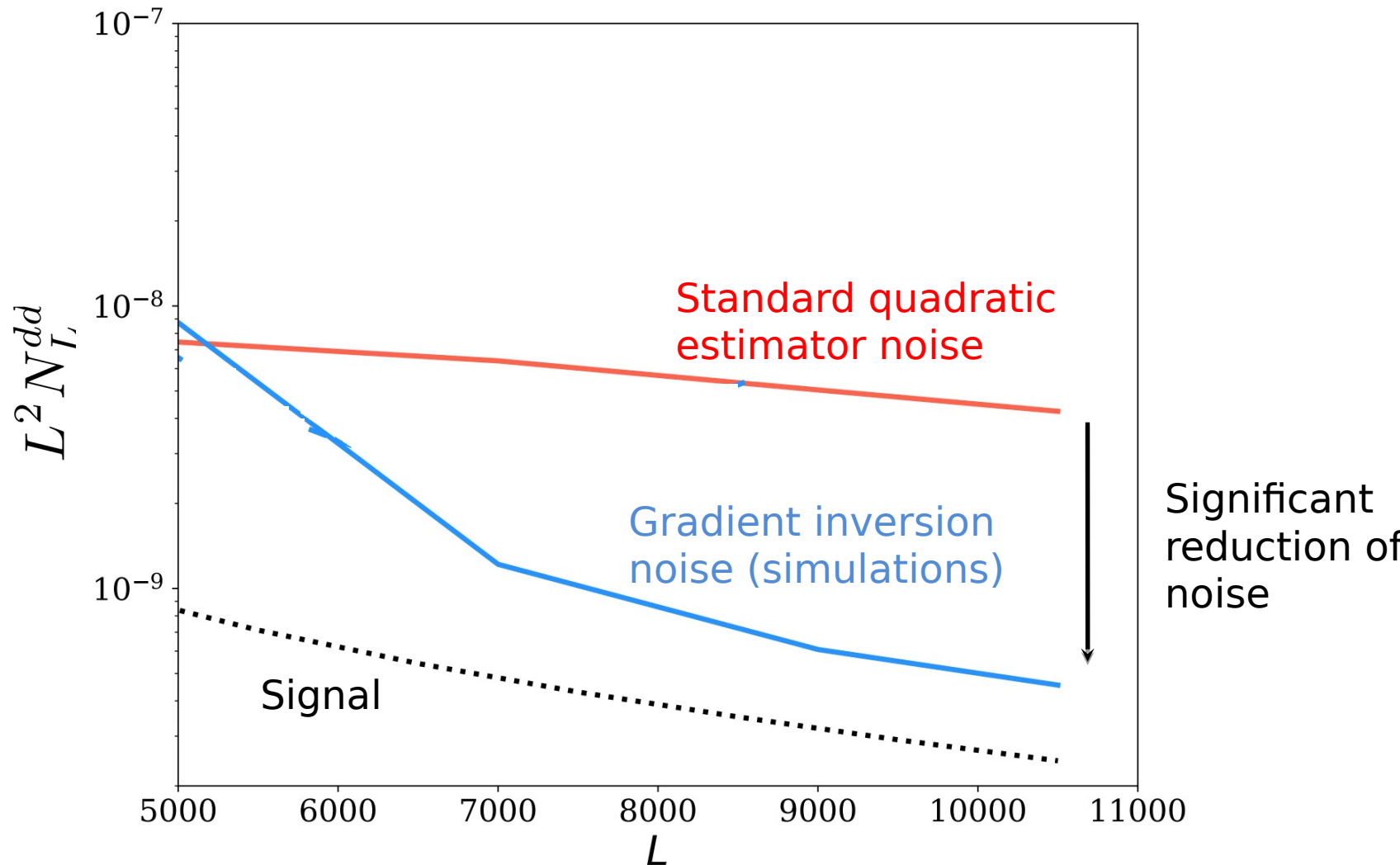
Reconstruction on ultra-small scales ($L \gtrsim 5000$) for S4:
GI does well in large gradient regions

[Hadzhiyska et al. 2019]

Successful Validation: reconstruction x input correlation

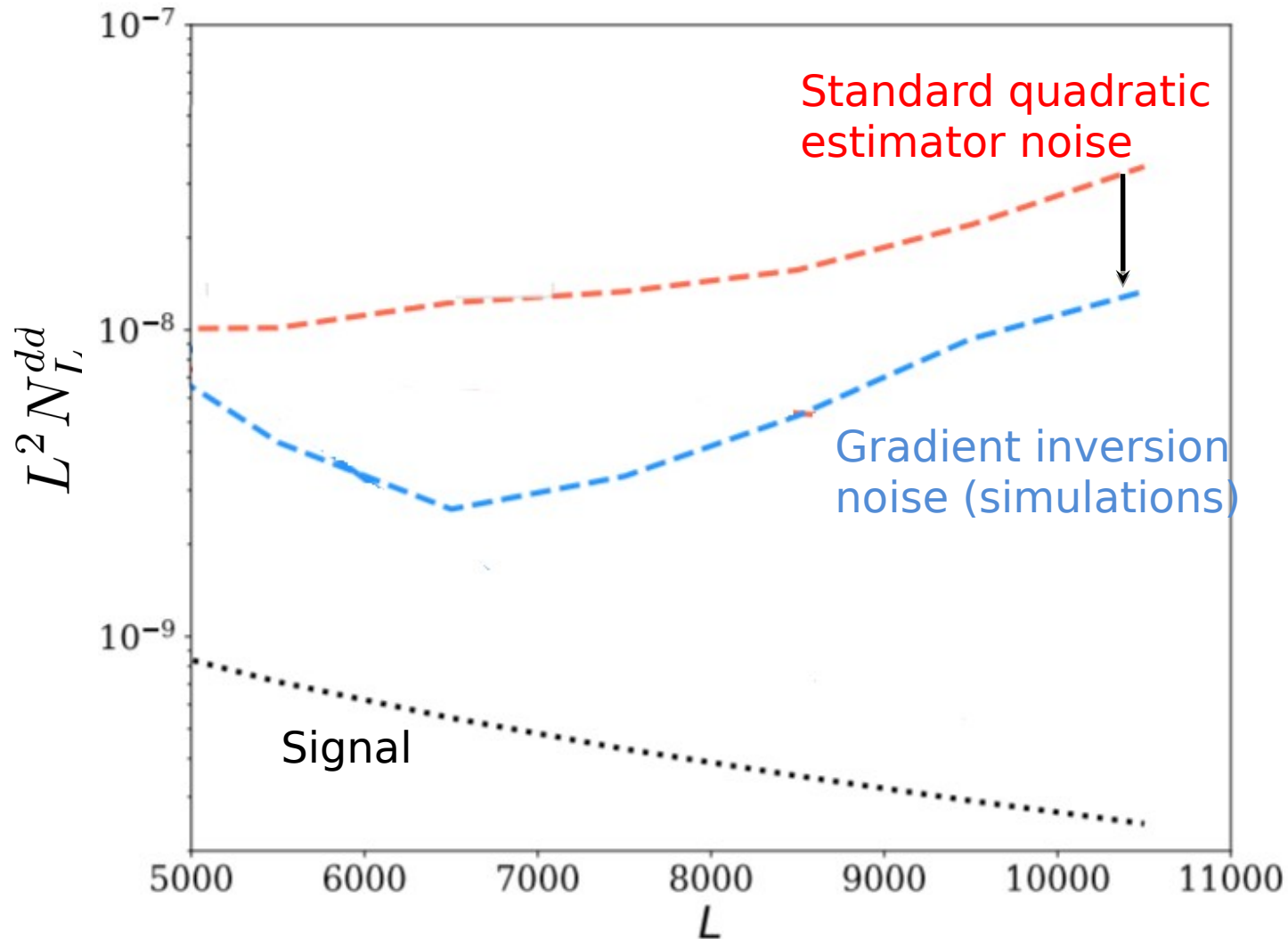


Significant Improvements Possible? Ultra-low noise errors (0.1 $\mu\text{K}'$)



- Error on the measurements **smaller** for GI compared with QE

Significant Improvements Possible? CMB-S4 wide noise errors (1 $\mu\text{K}'$)



- Error on the measurements **even smaller** for GI compared with QE

Significant Improvements Possible?

Signal-to-noise ratio

- Estimate the signal-to-noise ratio for the auto- and cross-correlation of the convergence field:

$$\text{SNR}^2 = \sum_{ij} C_L^{i\kappa\kappa} \widehat{\text{Cov}}_{ij}^{-1} C_L^{j\kappa\kappa}$$

- Significant improvement compared to QE (on $L > 4000$).

| SNR | | UL | S4-like | SO-like |
|--------------|---------|------|---------|---------|
| C_L^{dd} → | Auto QE | 205 | 100 | 7 |
| | Auto GI | 1515 | 360 | 30 |

Factor of 4 improvement!

Caveats and next steps

- Suggest that a better estimator exists on small scales!
 - a. reachable with CMB-S4 LAT survey
- Foreground noise (CIB, tSZ, kSZ)
 - a. proposed ideas for how to clean
 - b. polarization does not suffer from that
- Optimal method: maximum likelihood estimator can bridge the gap on intermediate and small scales (in progress)

Multi-frequency approaches to cleaning are available!

Has a blackbody frequency dependence, but is not correlated with the CMB gradient.

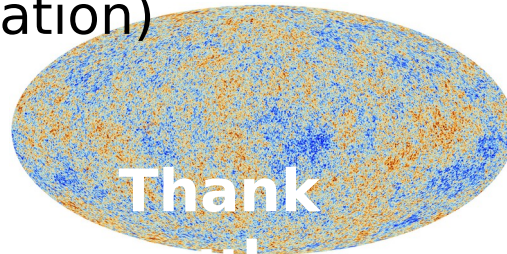
Outline

1. Motivation
2. Lensing reconstruction methods
 - a. Quadratic estimator (QE)
 - b. Gradient-inversion (GI)
3. Caveats and next steps
- 4. Summary**

Summary

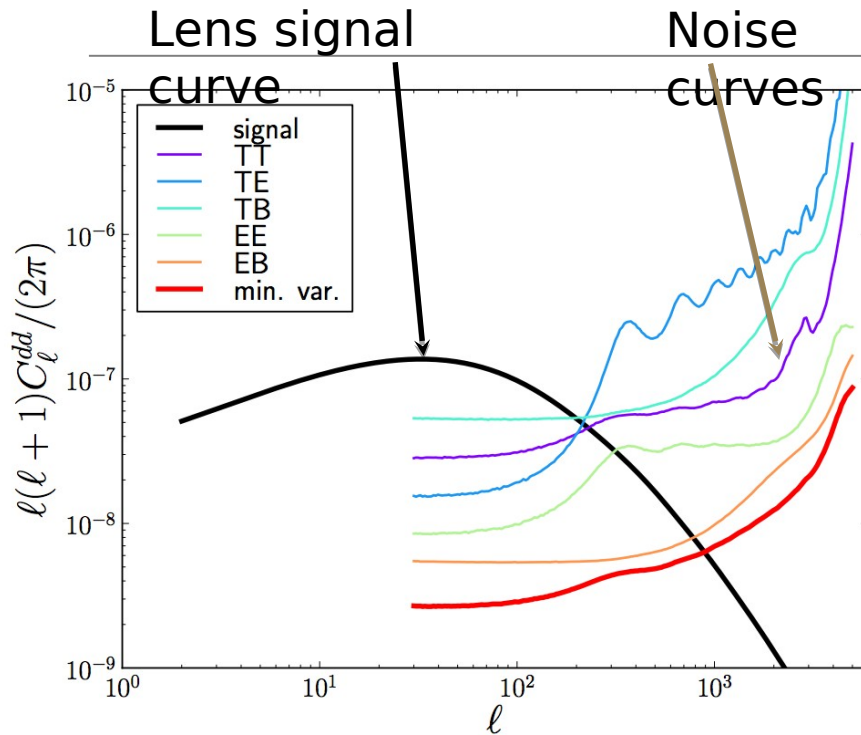
arXiv:1905.04217

1. There is lots of unexplored lensing potential on small scales
2. Advantages of small-scale lensing:
 - a. axion physics, warm dark matter (WDM)
 - b. cross-correlations with galaxies, polarization
 - c. assembly bias (one-halo term)
3. Proposed a new estimator for very small scales
4. There are some caveats that can be overcome (foreground cleaning, polarization)



Backup Slides

Small-scale puzzle



Noise for CMB-S4 (Schaan et al. 2017)

- A puzzle: quadratic estimator noise gets large – seemingly cannot probe tiny CMB lenses / scales

Lensing Measurement with the Quadratic Estimator

Lensing changes known homogeneous statistics: introduces new correlations

$$\langle T(\mathbf{l}) T^*(\mathbf{l} - \mathbf{L}) \rangle \sim d(\mathbf{L})$$

T: temperature (Fourier mode)

l: wavenumber

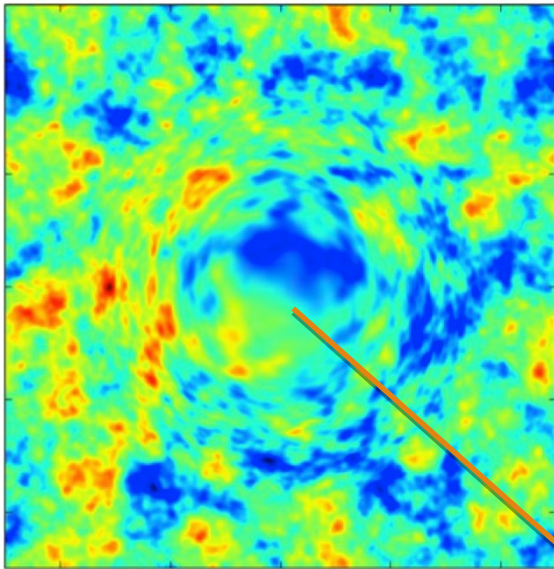
So: measure lensing by looking for these correlations with a **Quadratic Estimator** in the CMB fields:

$$\begin{aligned} \hat{d}(\mathbf{L}) &\sim \int d^2\mathbf{l} T(\mathbf{l}) T^*(\mathbf{l} - \mathbf{L}) \\ &\sim \text{FT}[T \nabla T] \end{aligned}$$

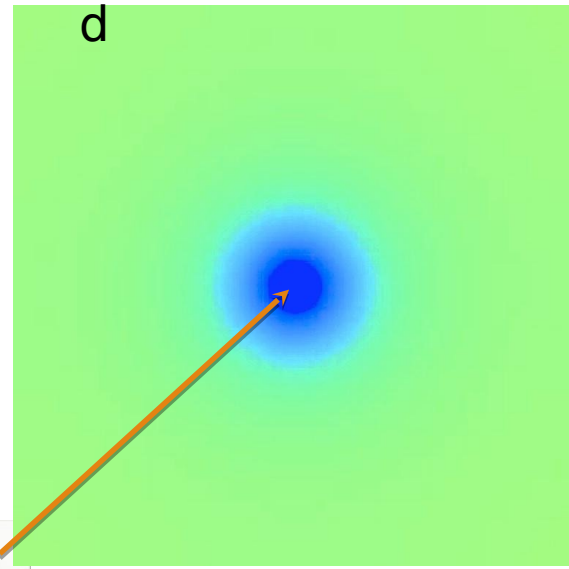
[Zaldarriaga, Seljak 1997, Hu, Okamoto 2002]

CMB Lensing Measurement: An Approximate Picture

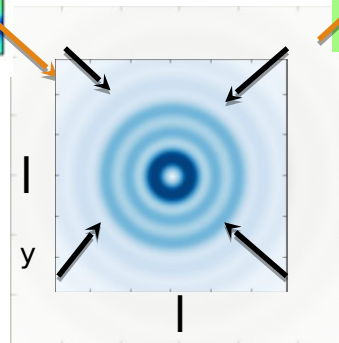
CMB temperature



Lensing deflection



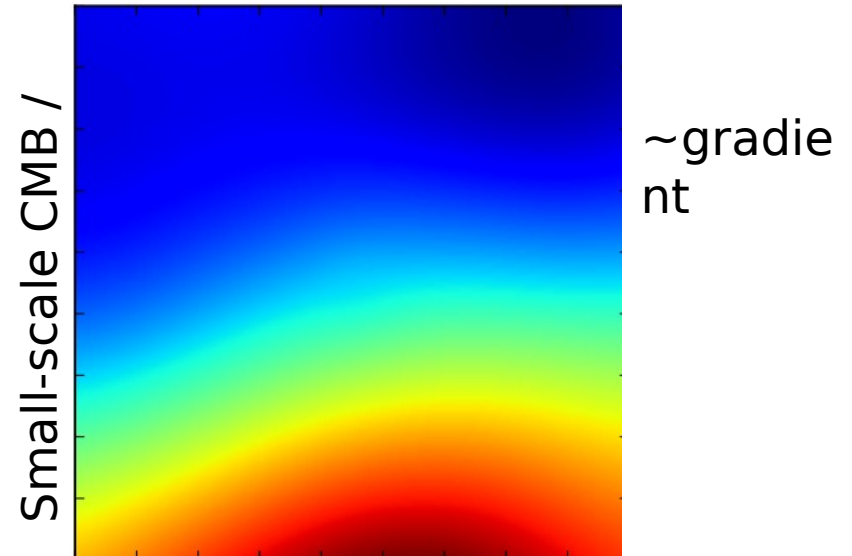
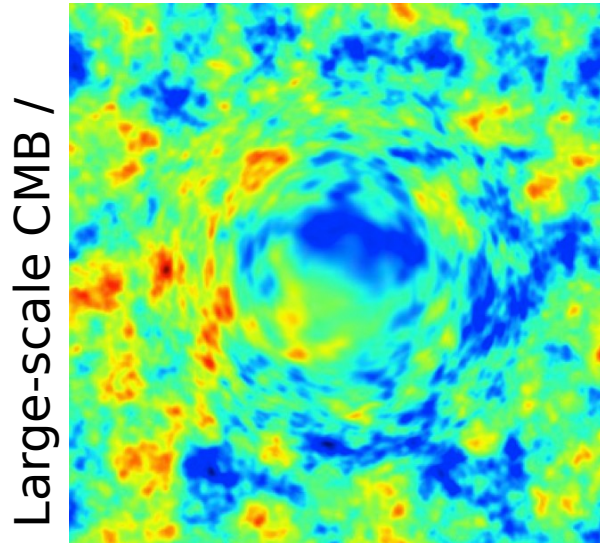
local 2D power spectrum



Infer lensing from
“stretching” of the local
CMB power spectrum
(+ shearing)

[Bucher et al. 2012]

The Simplicity of Small-scale CMB

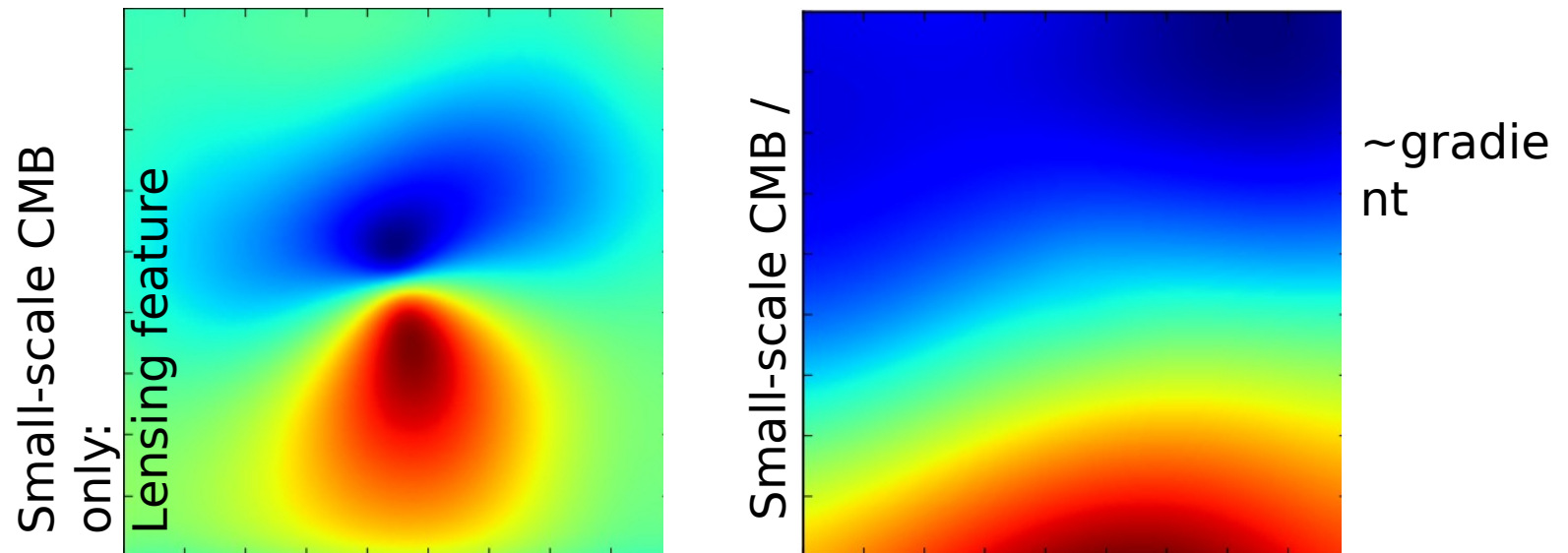


- On small scales, CMB gradient ∇T is effectively constant. Lensing expansion:

$$T(\mathbf{x}) = T^u(\mathbf{x} + \mathbf{d}) \approx T^u(\mathbf{x}) + \mathbf{d}(\mathbf{x}) \cdot \nabla T^u + \dots$$

Noise
Foreground
s

Gradient Inversion Lensing Estimation

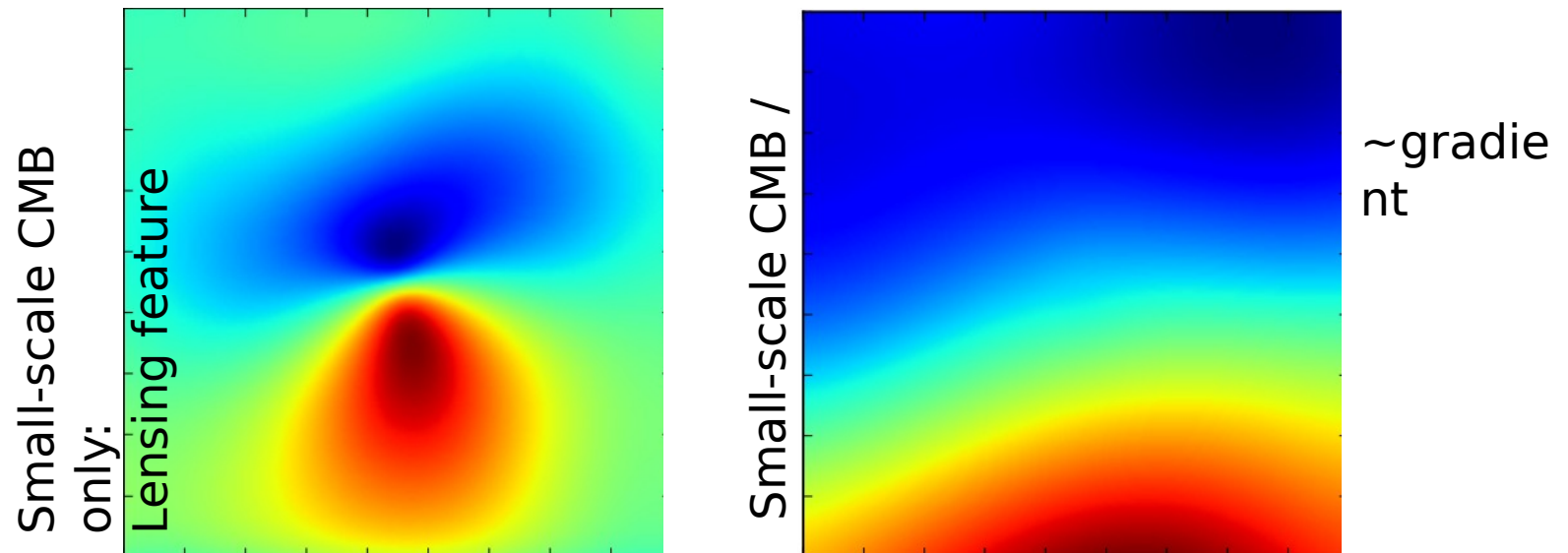


- Fourier transform with constant gradient:
$$T(\mathbf{L}) = d(\mathbf{L}) \times |\nabla T^u|_{\hat{\mathbf{n}}_{\mathbf{L}}}$$
- Suggests simple “gradient inversion” estimator:

$$\hat{d}(\mathbf{L}) = \frac{T(\mathbf{L})}{|\nabla T^u|_{\hat{\mathbf{n}}_{\mathbf{L}}}}$$

[Horowitz et al. 2017,
Zaldarriaga, Seljak
1997]

Gradient Inversion Lensing Estimation



- Fourier transform with constant gradient:

$$T(\mathbf{L}) = d(\mathbf{L}) \times |\nabla T^u|_{\hat{\mathbf{n}}_{\mathbf{L}}}$$
- Suggests simple “gradient inversion” estimator:

$$\hat{d}(\mathbf{L}) = \frac{T(\mathbf{L})}{|\nabla T^u|_{\hat{\mathbf{n}}_{\mathbf{L}}}}$$

← Not limited by cosmic variance;
SNR \sim local gradient

GI Extension to Large Maps and Spectra

- Expected noise is direction and position dependent

$$N^{dd}(\mathbf{L}, \mathbf{x}) \sim \frac{N_L^{TT}}{|\nabla T^u(\mathbf{x})|_{\hat{\mathbf{n}}_L}^2}$$

- Create inverse noise weight $W = N^{-1}$, allow gradient to slowly vary in final, continuous estimator:

$$d(\mathbf{L}) \sim FT \left[\frac{T(\mathbf{x})}{|\nabla T^u(\mathbf{x})|_{\hat{\mathbf{n}}_L}} W(\mathbf{L}, \mathbf{x}) \right]$$

[Hadzhiyska et al. 2019]