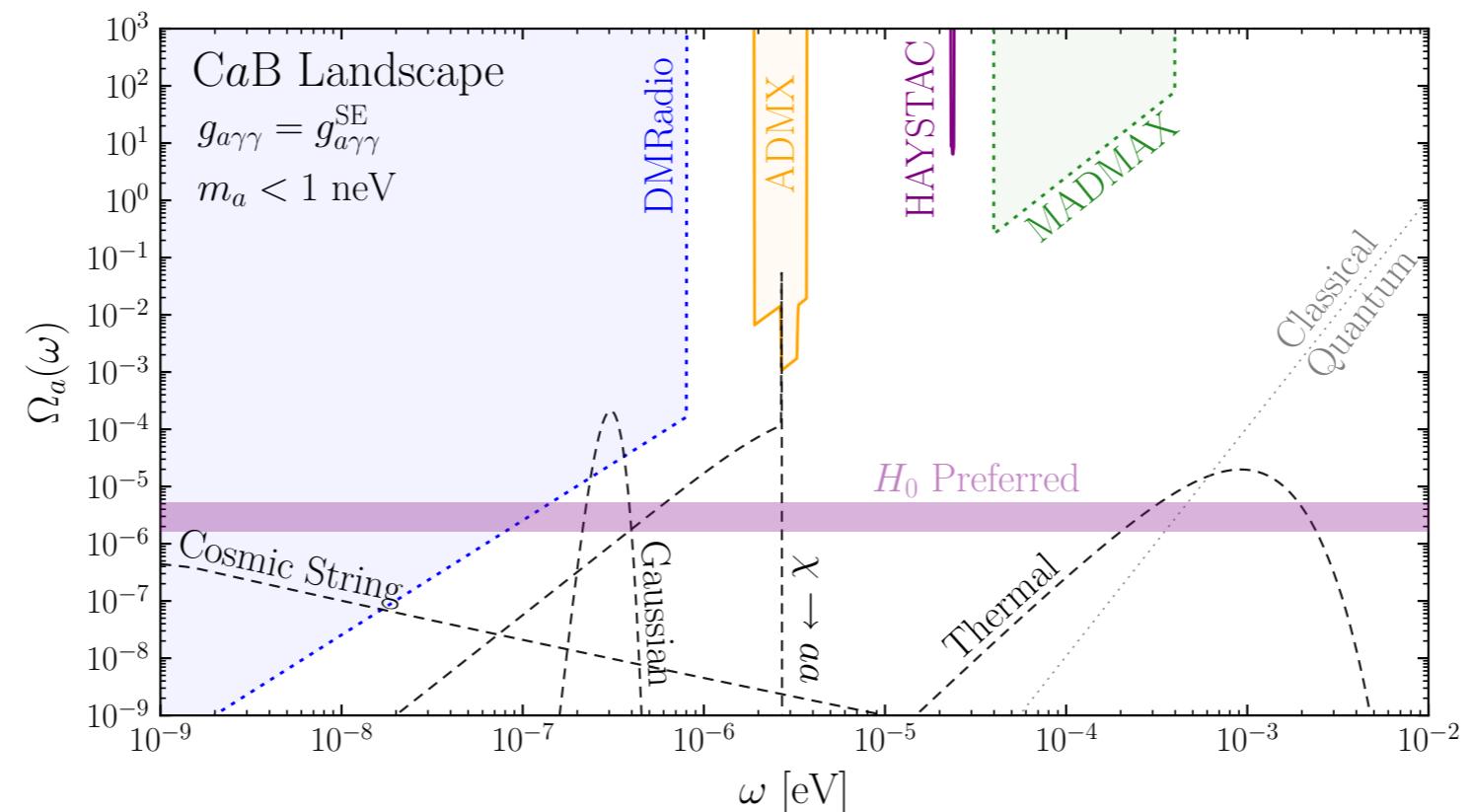


# The Cosmic Axion Background

NICK RODD | CMB-S4 COLLABORATION MEETING | 10 AUGUST 2021



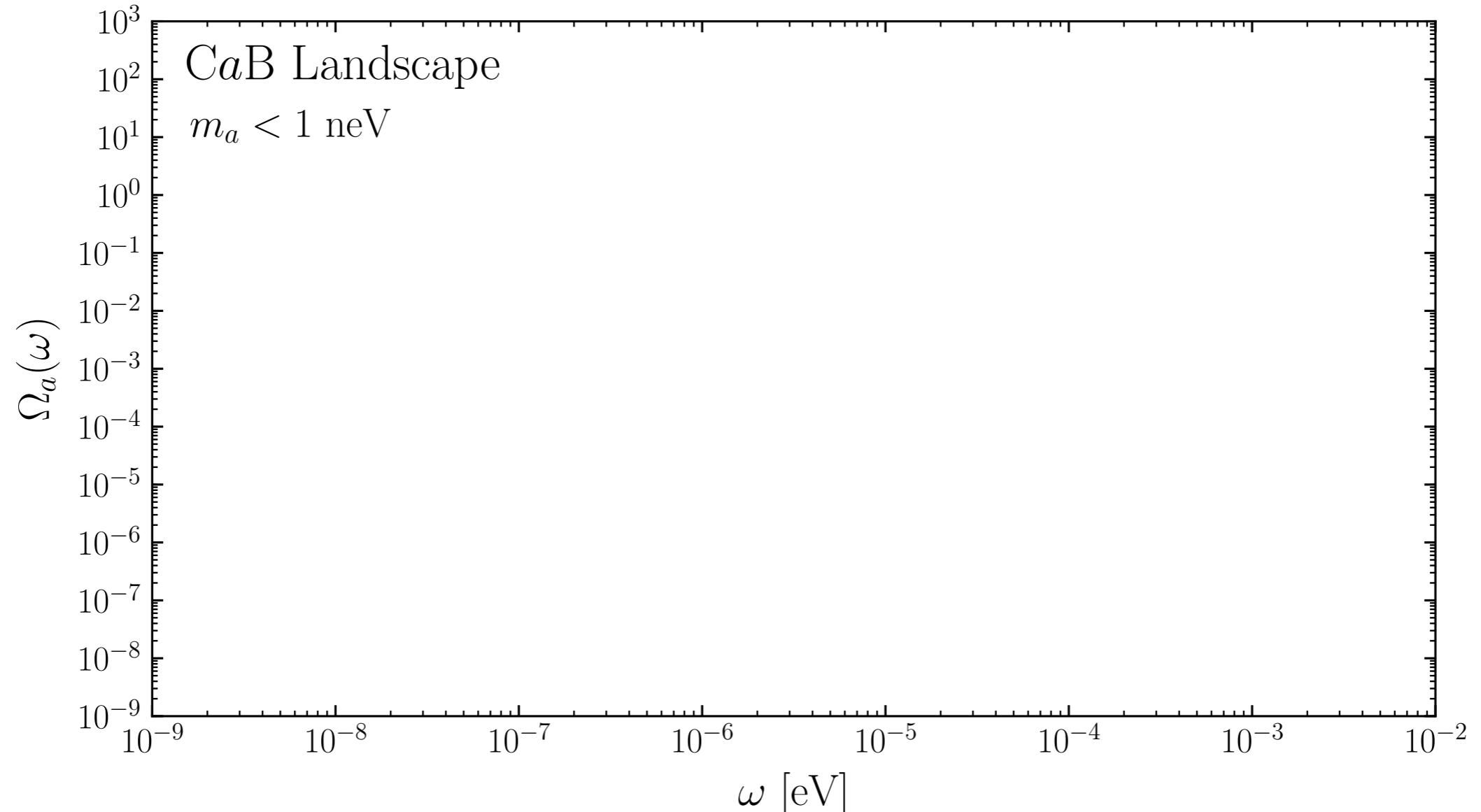
PRD 2021 (Editors' Suggestion) 2101.09287  
w/ Jeff Dror & Hitoshi Murayama



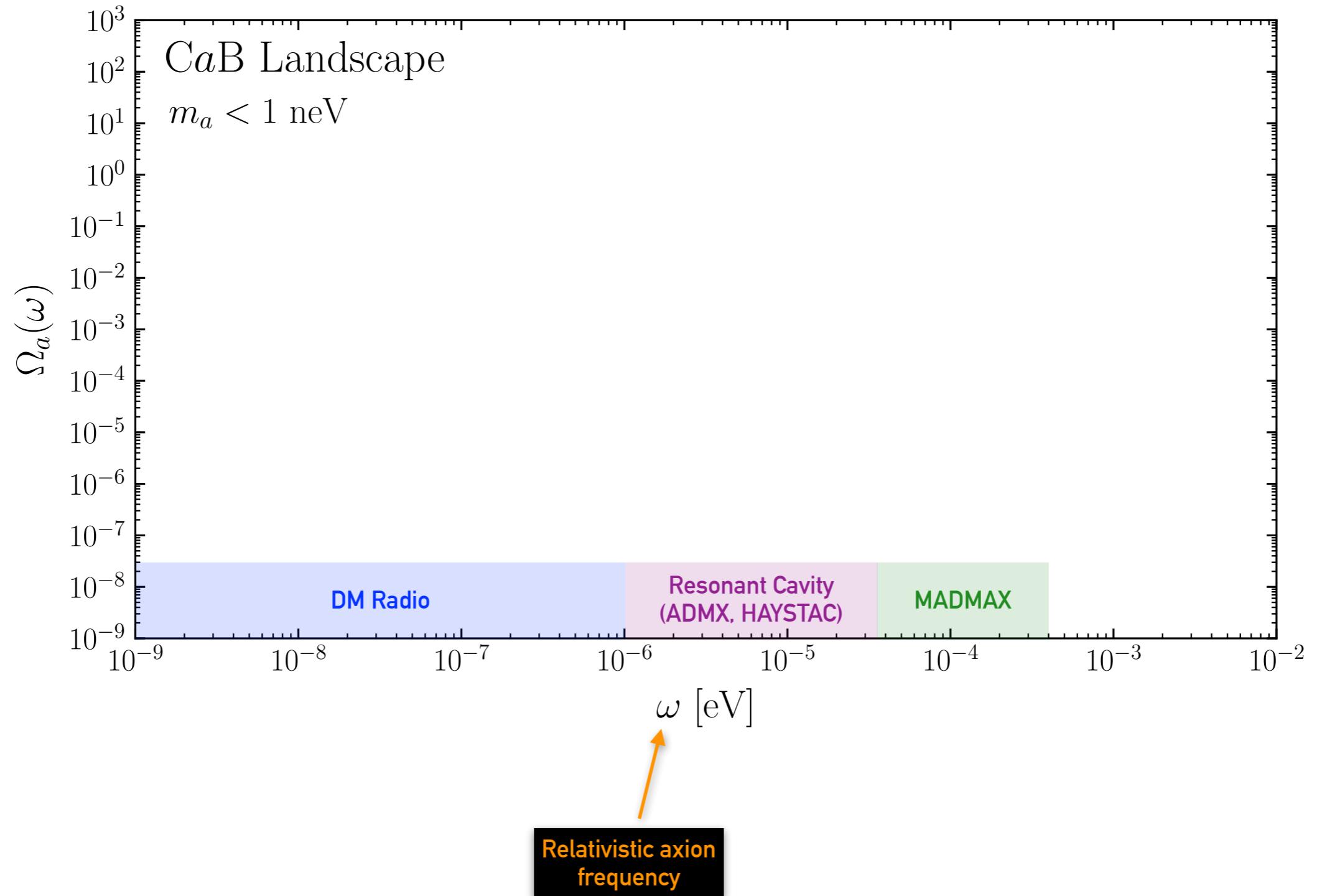
# The Cosmic Axion Background

**Can we detect relativistic axions that  
are a relic of the early Universe with  
axion haloscopes?**

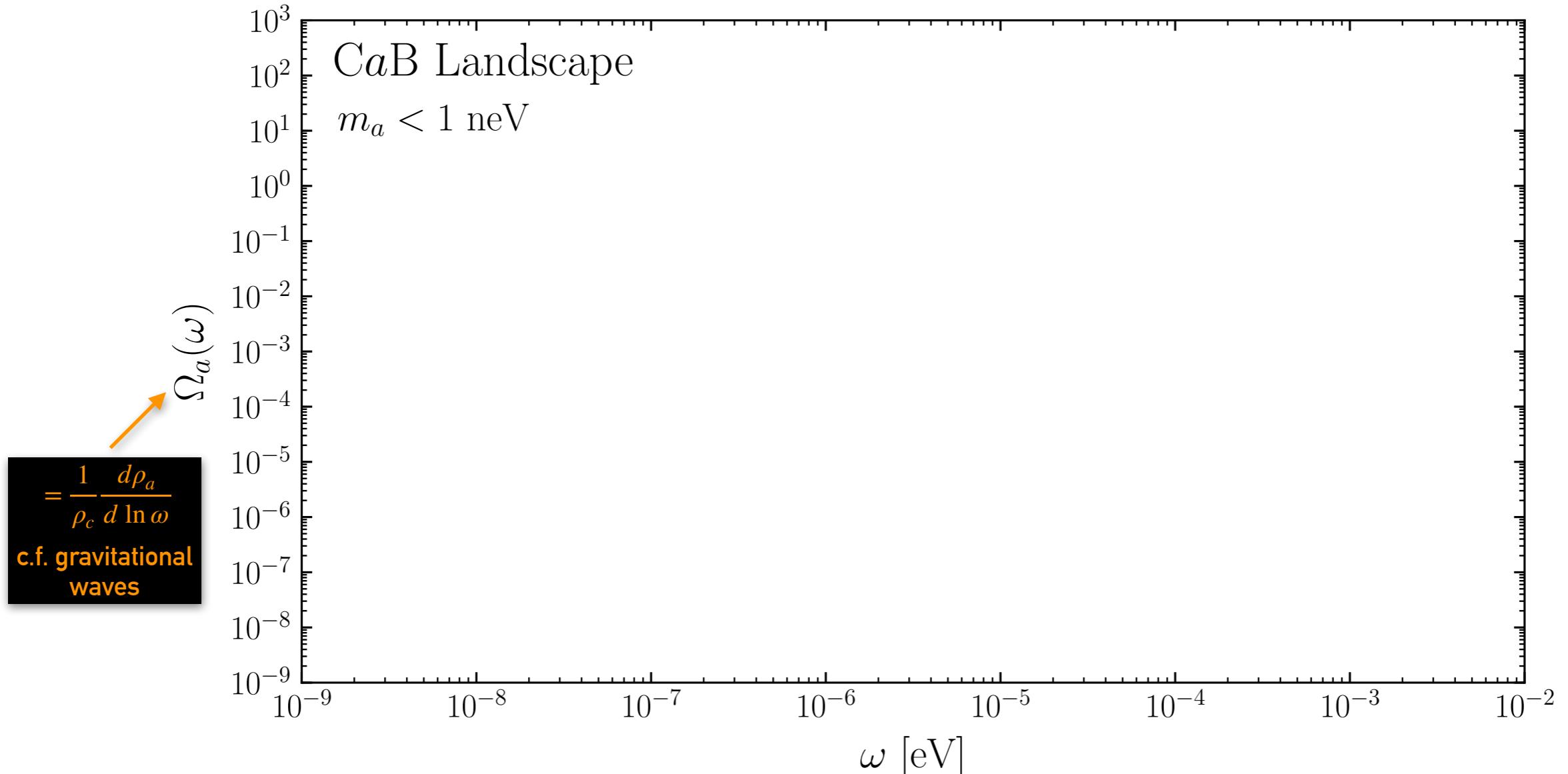
# Landscape



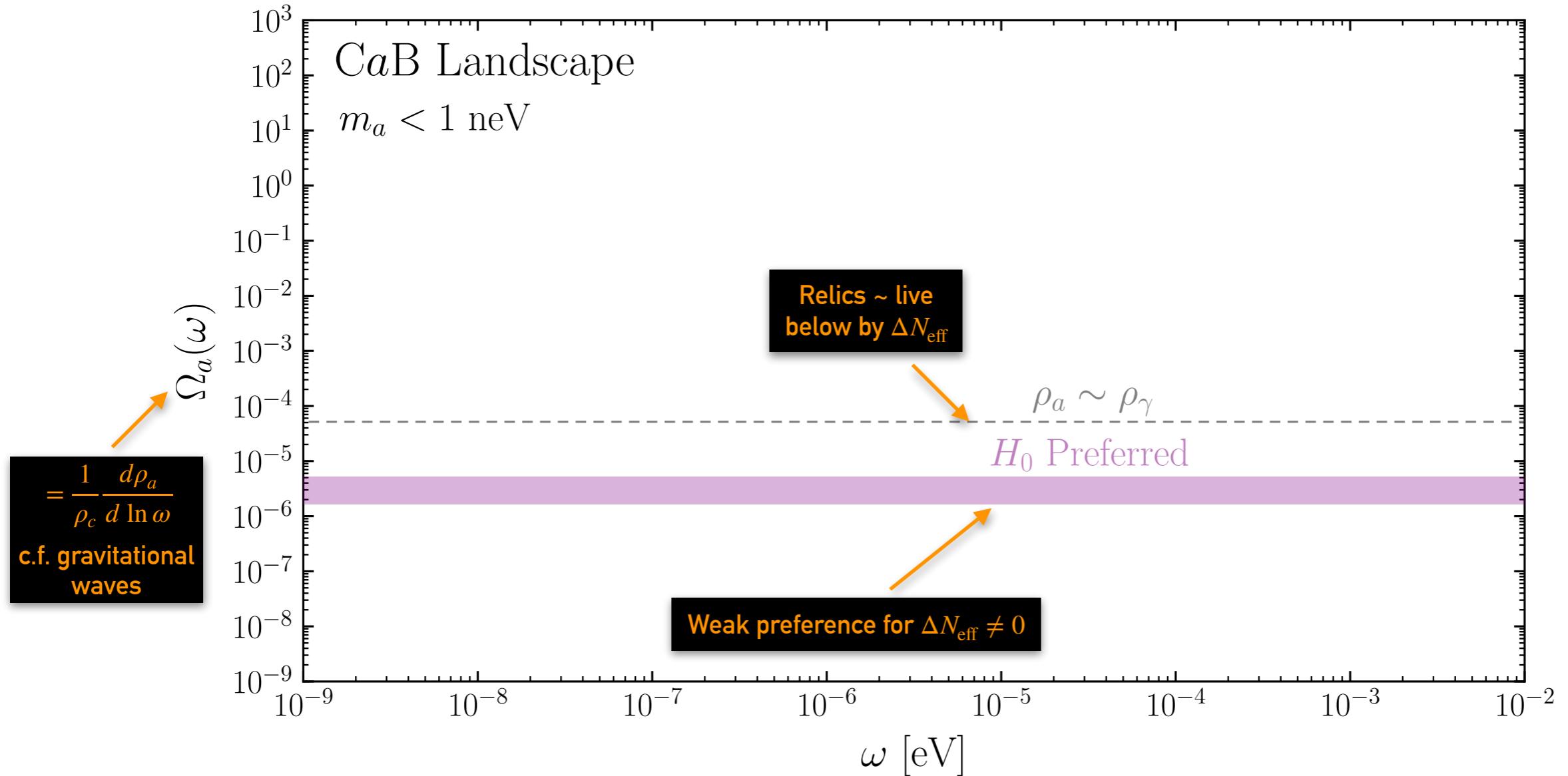
# Landscape



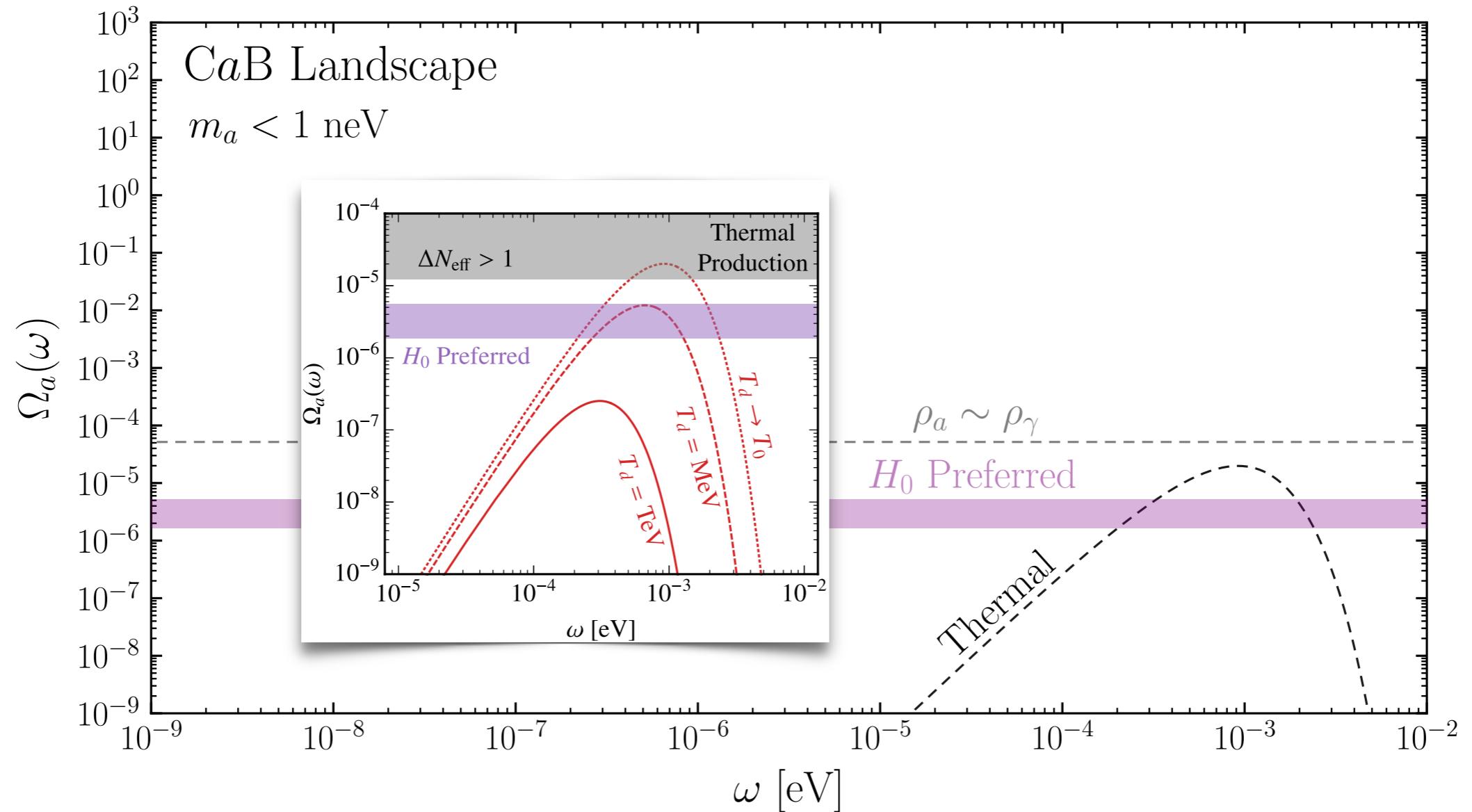
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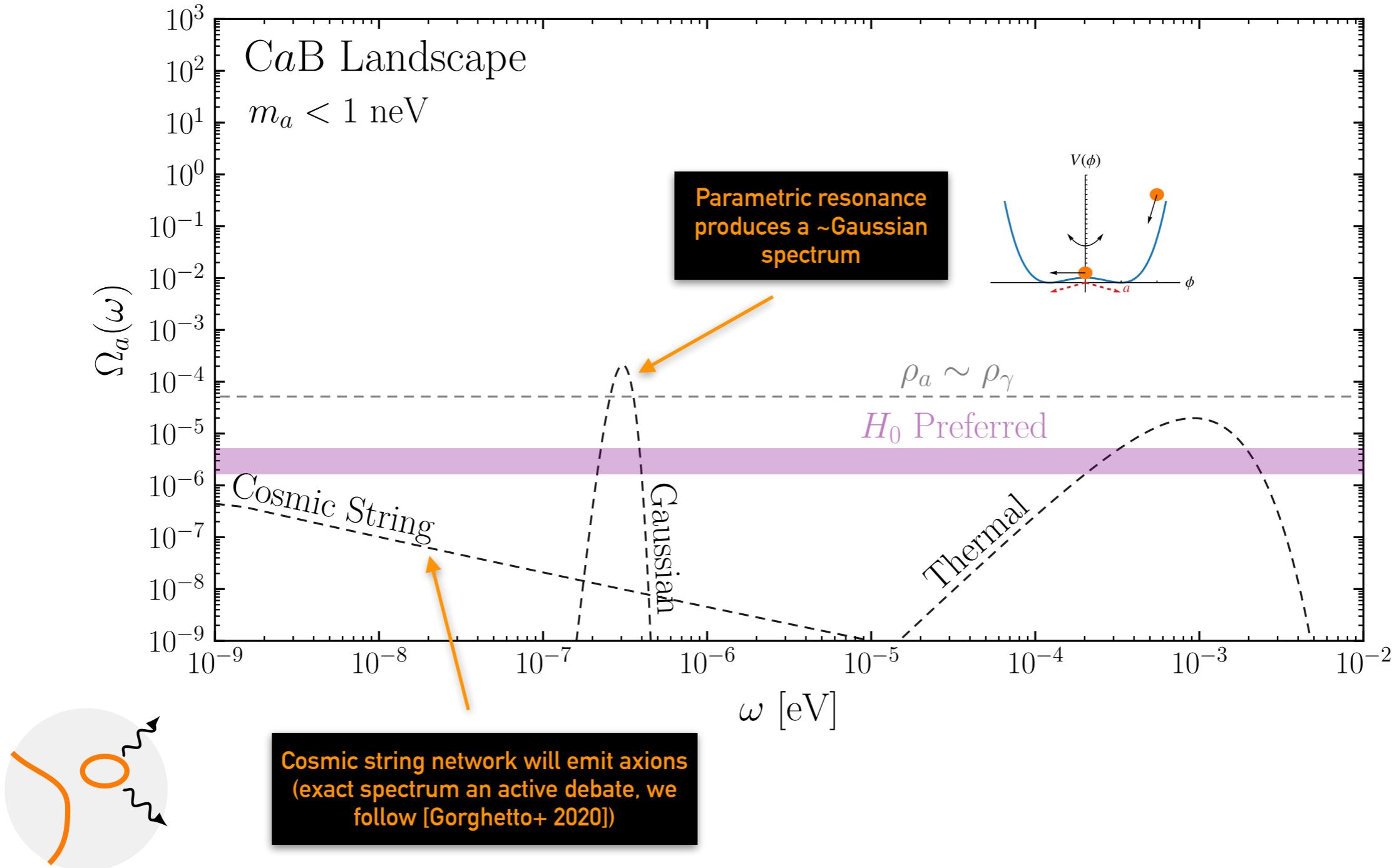
# Landscape



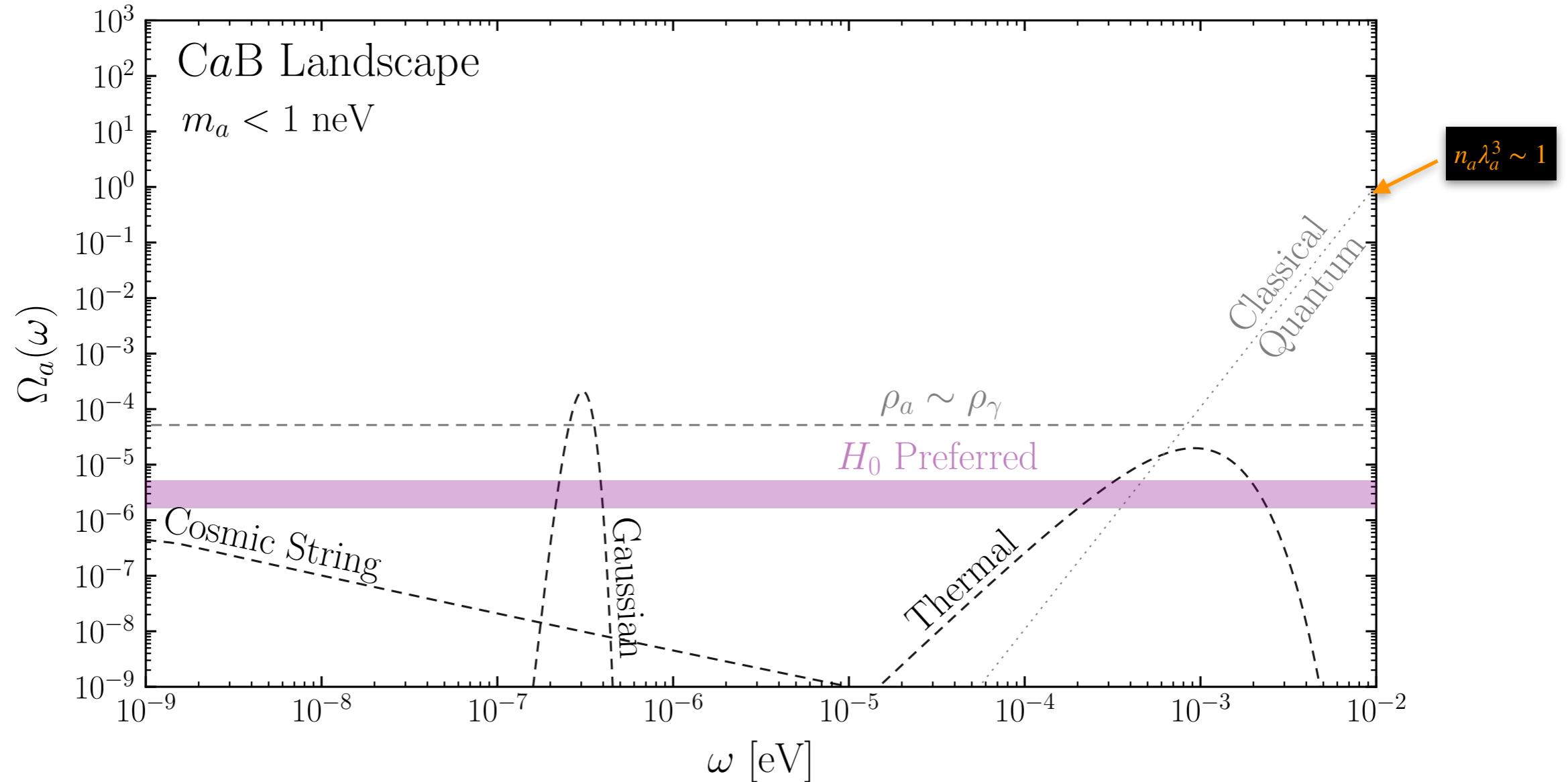
# Landscape



# Landscape

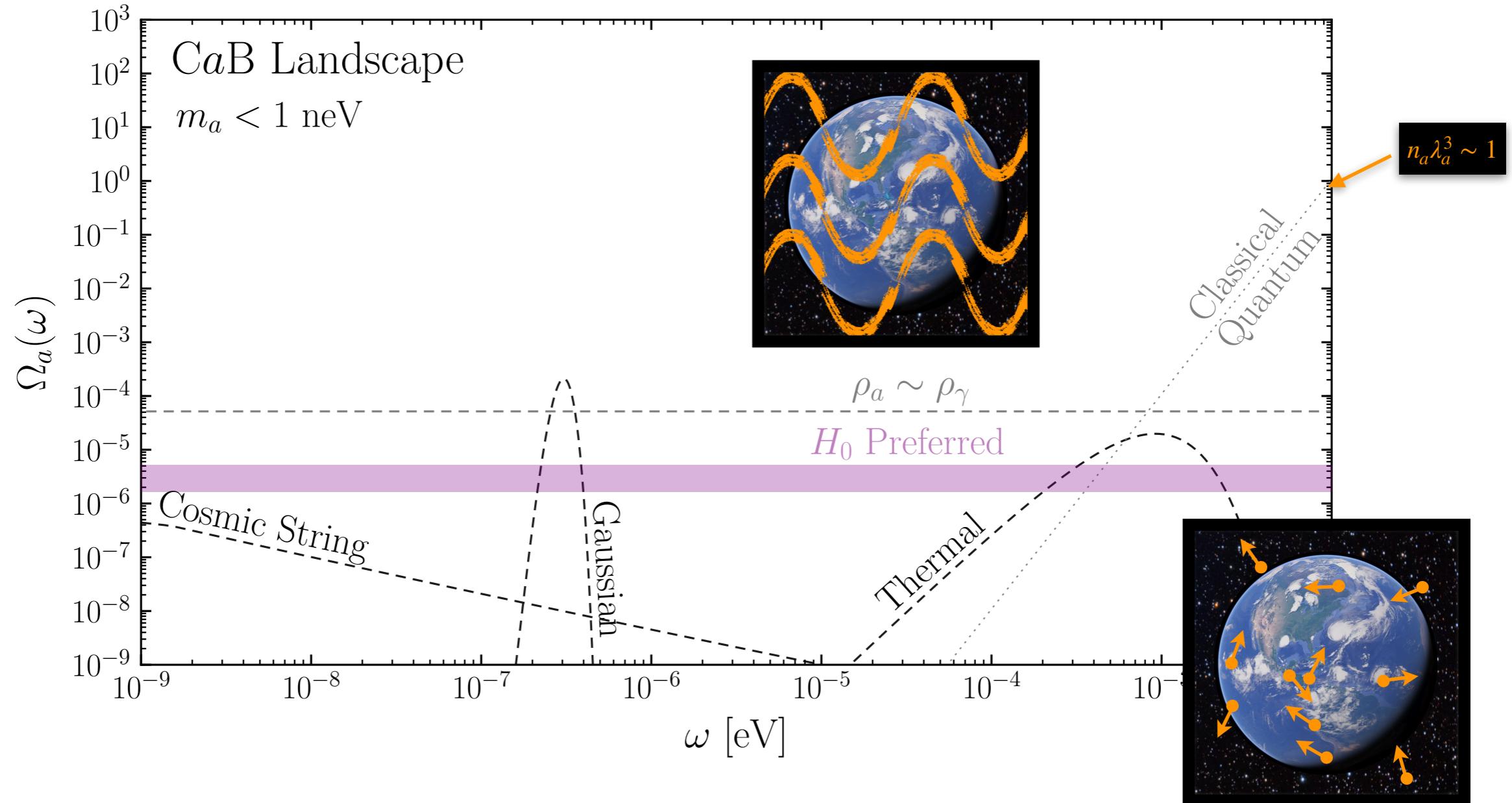


# Landscape



# Landscape

**Classical wave description applies**



# Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

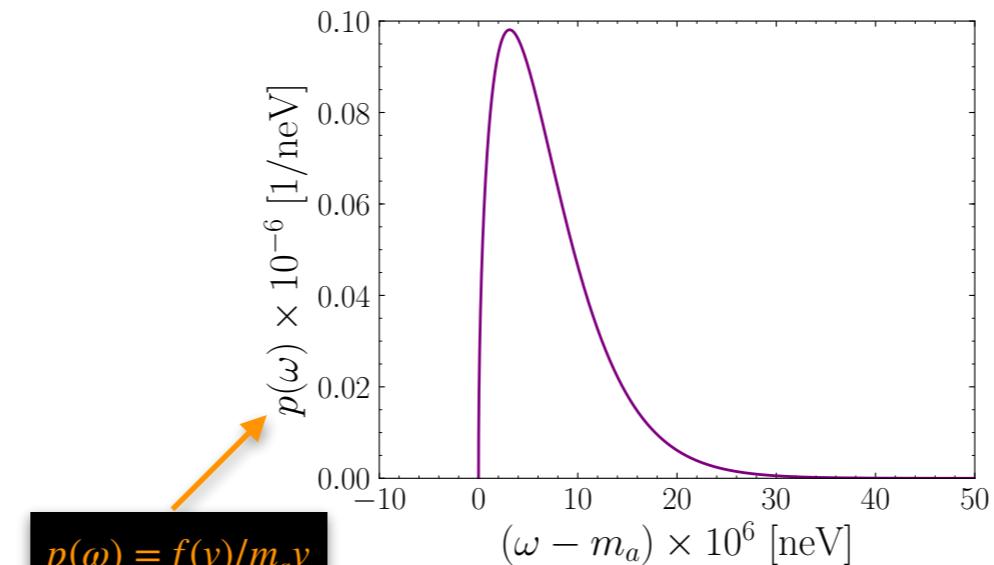
Sampled from frequency  
distribution  $p(\omega)$

Random phase

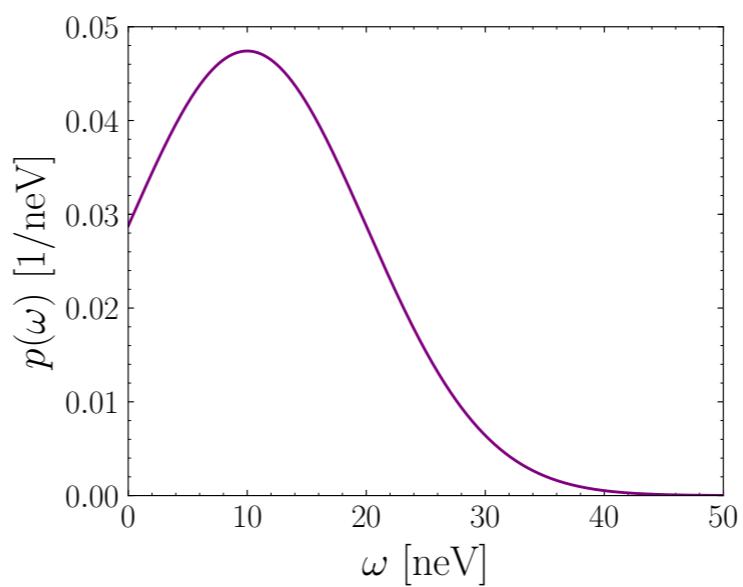
# Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

**Dark  
Matter**



**CaB**

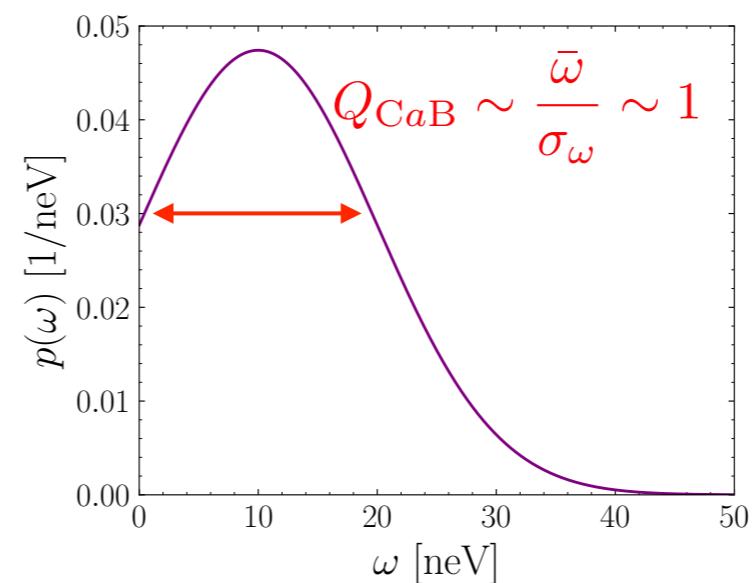
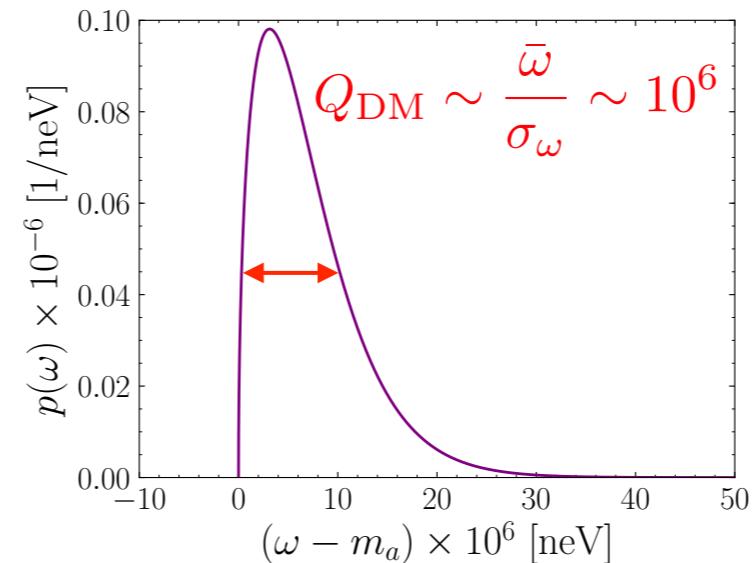


# Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

Dark  
Matter

**CaB**

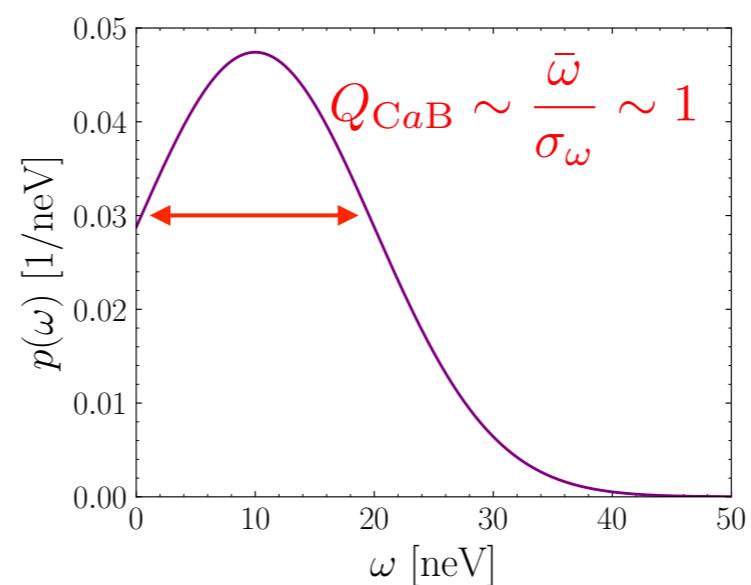
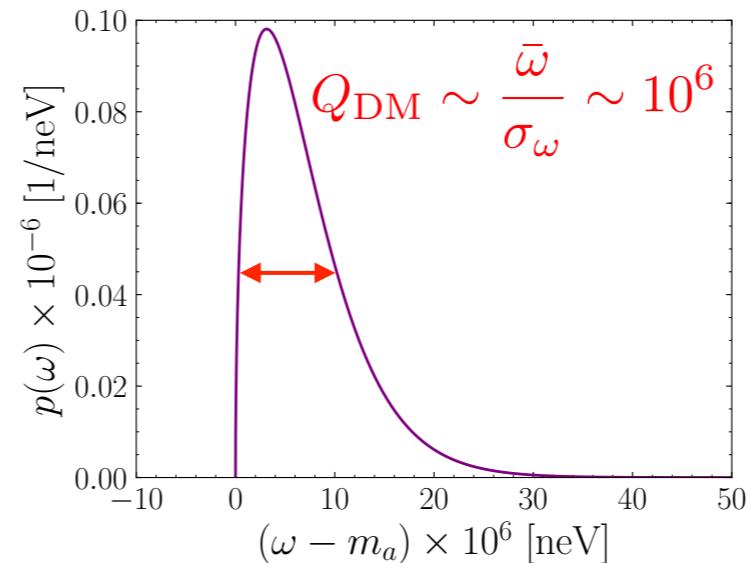


# Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

Dark  
Matter

CaB



Much broader signal -  
existing searches would  
throw out as background

# Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

## Accessible power in the axion field

Power spectral density -  
measures power at a  
given frequency

$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_a^2 \rho_a Q_a}{\bar{\omega}}$$

Approximate  $p(\omega) \sim Q_a/\bar{\omega}$



# Rough Sensitivity

Estimate sensitivity by matching power  $P_{\text{DM}} = P_{\text{CaB}}$

$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_{a\gamma\gamma}^2 \rho_a Q_a}{\bar{\omega}}$$

# Rough Sensitivity

**Estimate sensitivity by matching power  $P_{\text{DM}} = P_{\text{CaB}}$**

$$\text{Single bin: } (g_{a\gamma\gamma}^{\lim})^2 \rho_{\text{DM}} Q_{\text{DM}} = (g_{a\gamma\gamma}^{\text{SE}})^2 \rho_a Q_{\text{CaB}}$$

Dark Matter sensitivity

Star Emission sensitivity (e.g. CAST)

$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_{a\gamma\gamma}^2 \rho_a Q_a}{\bar{\omega}}$$

# Rough Sensitivity

**Estimate sensitivity by matching power  $P_{\text{DM}} = P_{\text{CaB}}$**

**Single bin:**  $(g_{a\gamma\gamma}^{\lim})^2 \rho_{\text{DM}} Q_{\text{DM}} = (g_{a\gamma\gamma}^{\text{SE}})^2 \rho_a Q_{\text{CaB}}$

$$\text{All bins: } \rho_a = \rho_{\text{DM}} \left( \frac{g_{a\gamma\gamma}^{\lim}}{g_{a\gamma\gamma}^{\text{SE}}} \right)^2 \sqrt{\frac{Q_{\text{DM}}}{Q_{\text{CaB}}}}$$

↑  
**Lose:**  $\rho_a \ll \rho_{\text{DM}}$

↑  
**Win:**  $g_{a\gamma\gamma}^{\lim} \ll g_{a\gamma\gamma}^{\text{SE}}$

↑  
**Lose:**  $Q_{\text{CaB}} \ll Q_{\text{DM}}$

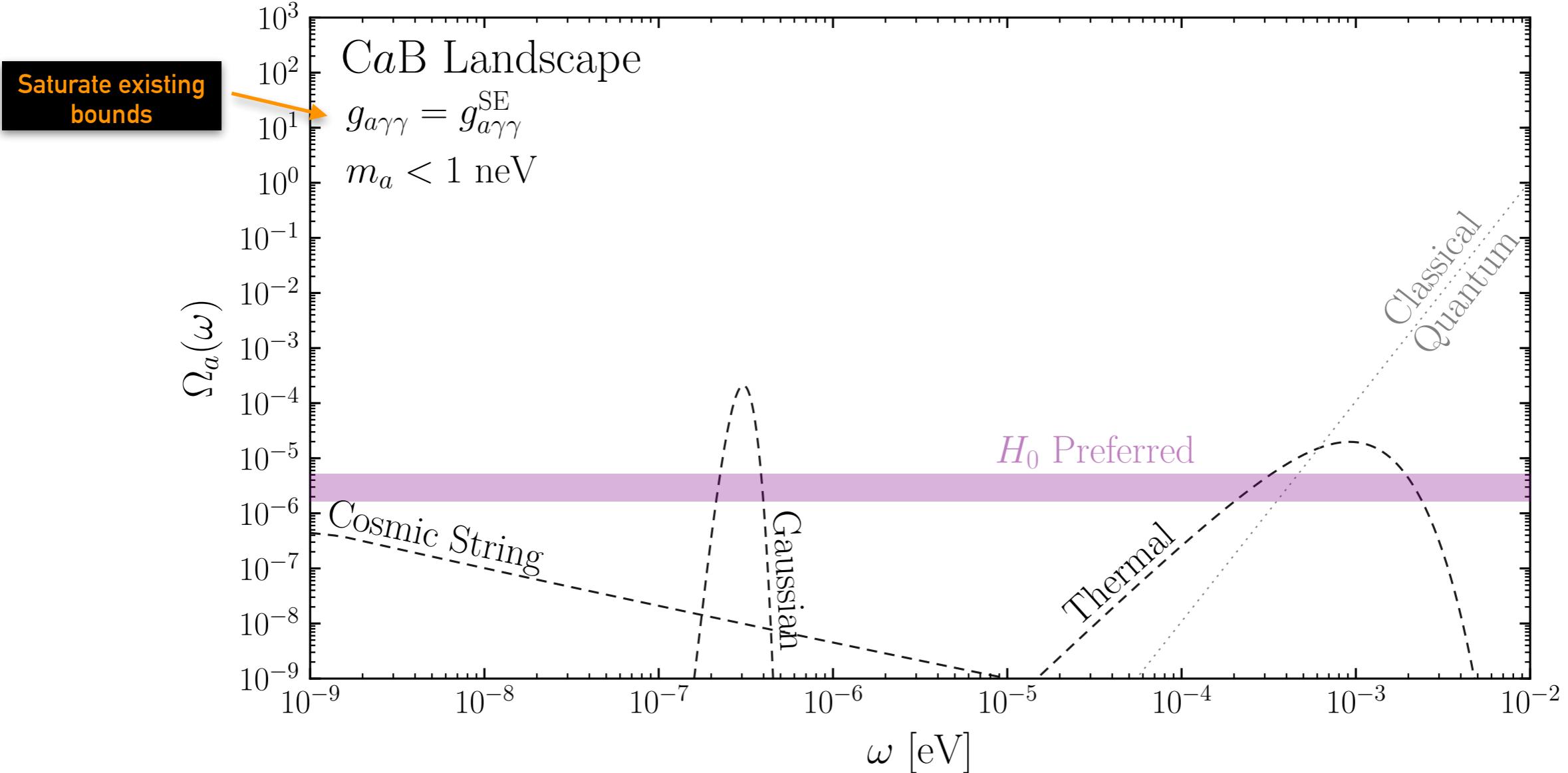
$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_{a\gamma\gamma}^2 \rho_a Q_a}{\bar{\omega}}$$

# Rough Sensitivity

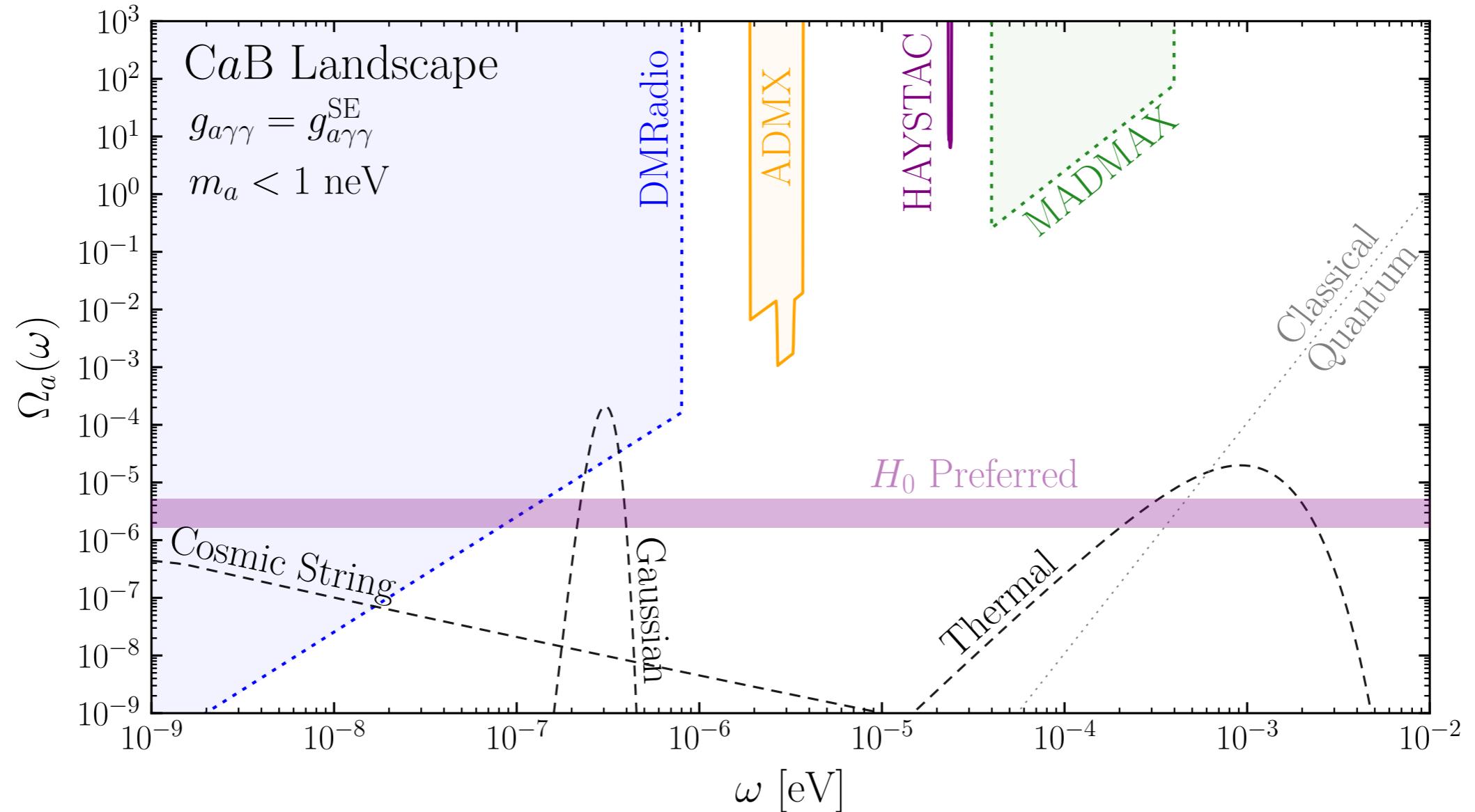
$$\rho_a = \rho_{\text{DM}} \left( \frac{g_{a\gamma\gamma}^{\lim}}{g_{a\gamma\gamma}^{\text{SE}}} \right)^2 \sqrt{\frac{Q_{\text{DM}}}{Q_{\text{CaB}}}}$$

Parametric scaling confirmed by detailed calculations for both resonant and broadband instruments

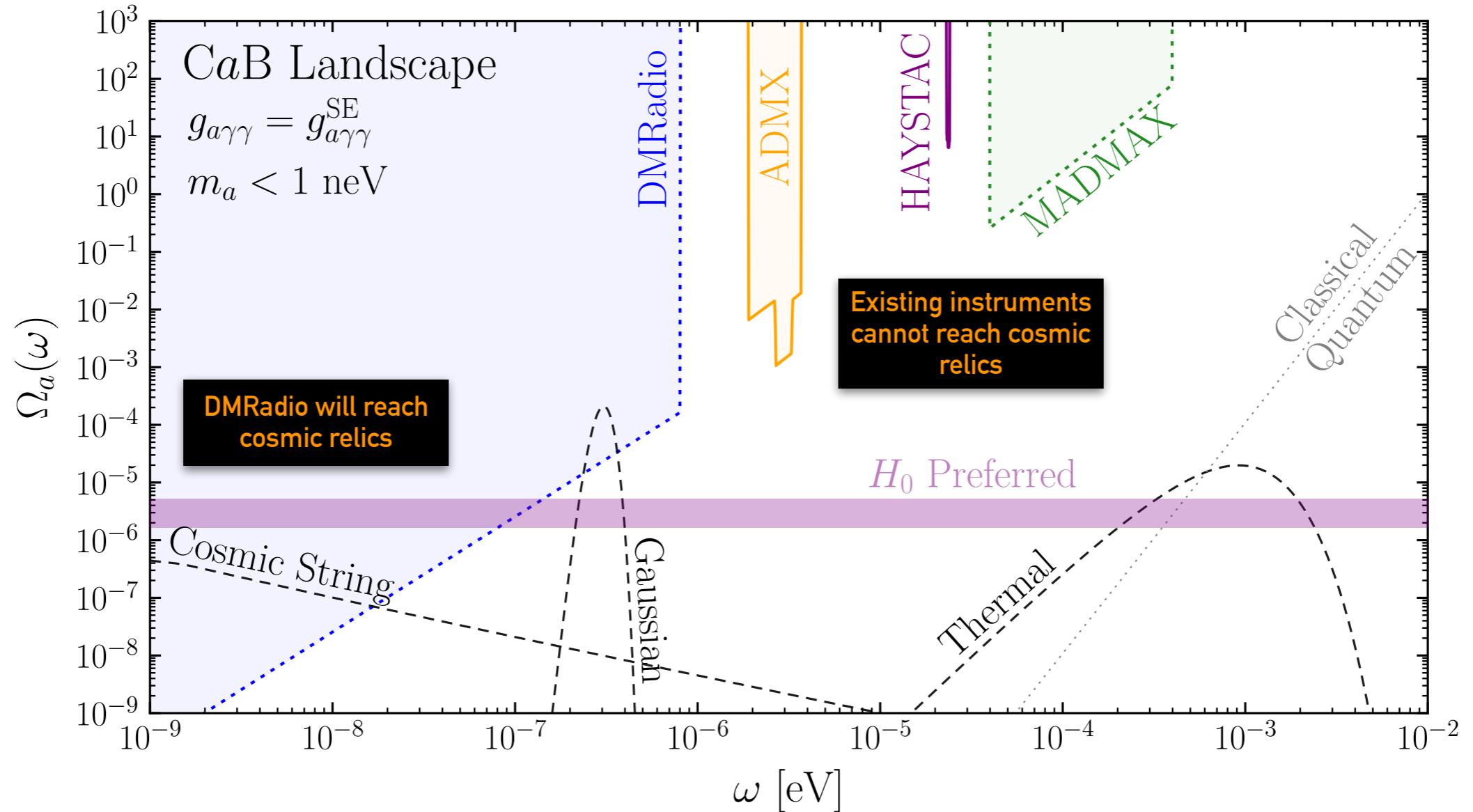
# Experimental Landscape



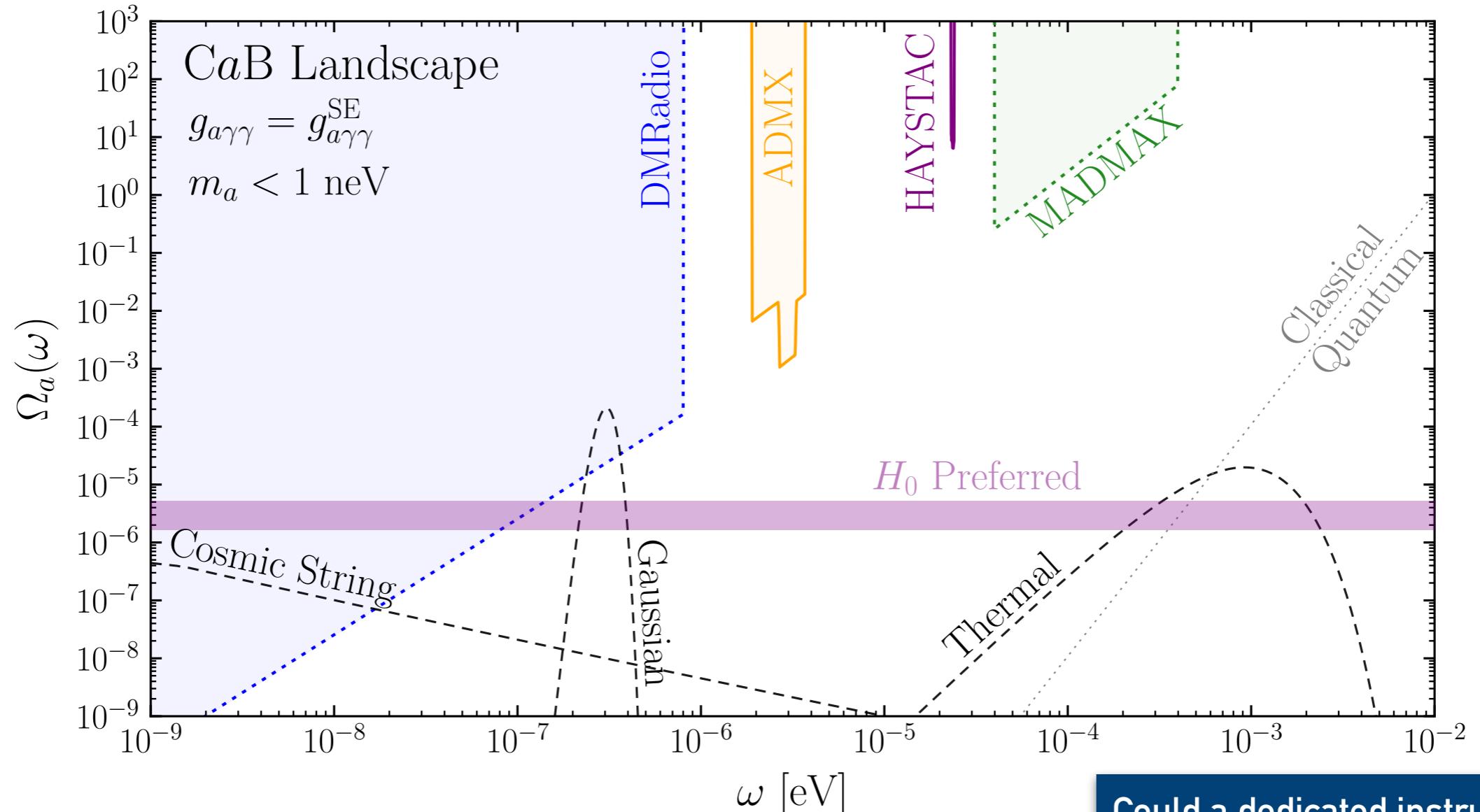
# Experimental Landscape



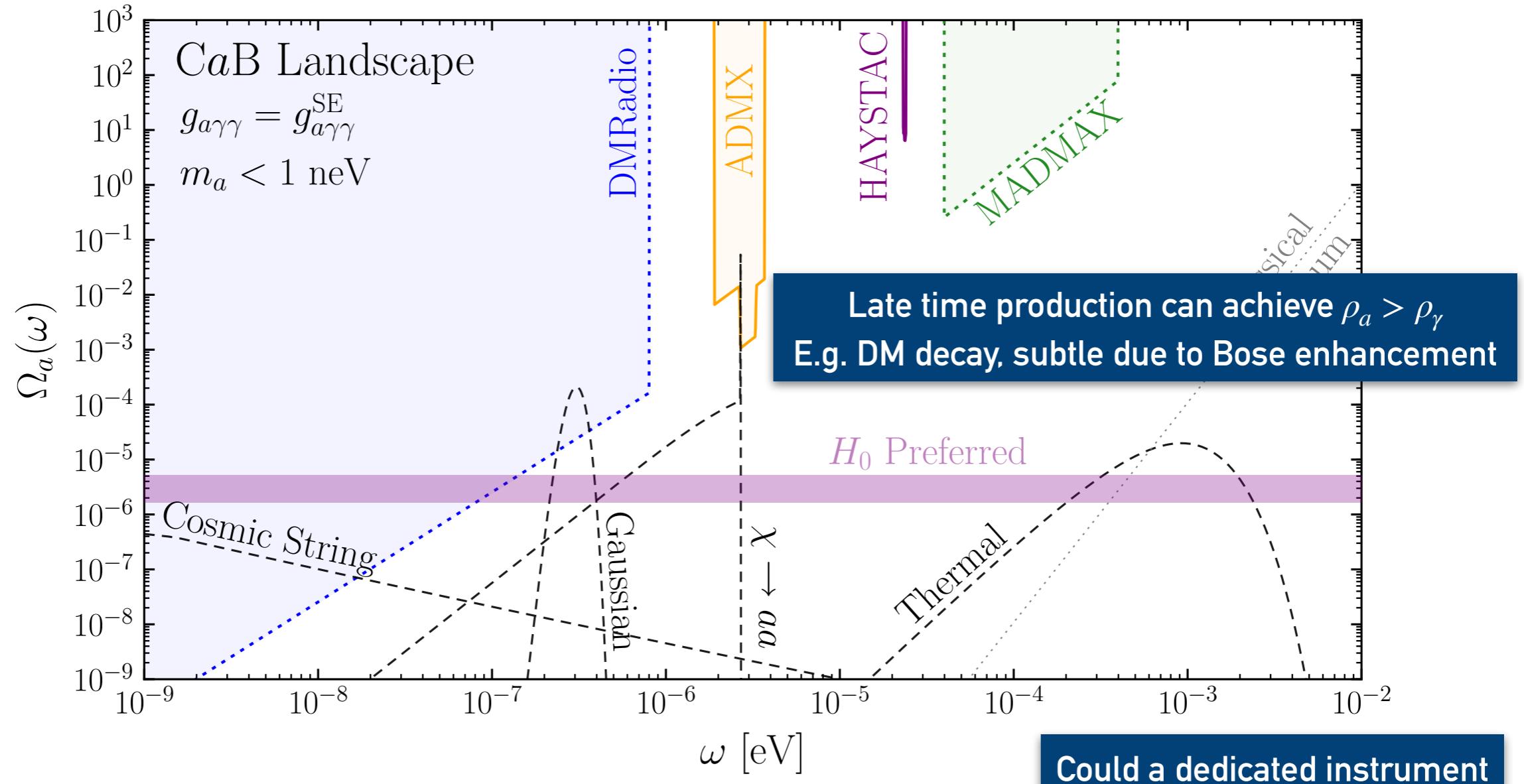
# Experimental Landscape



# Future Directions



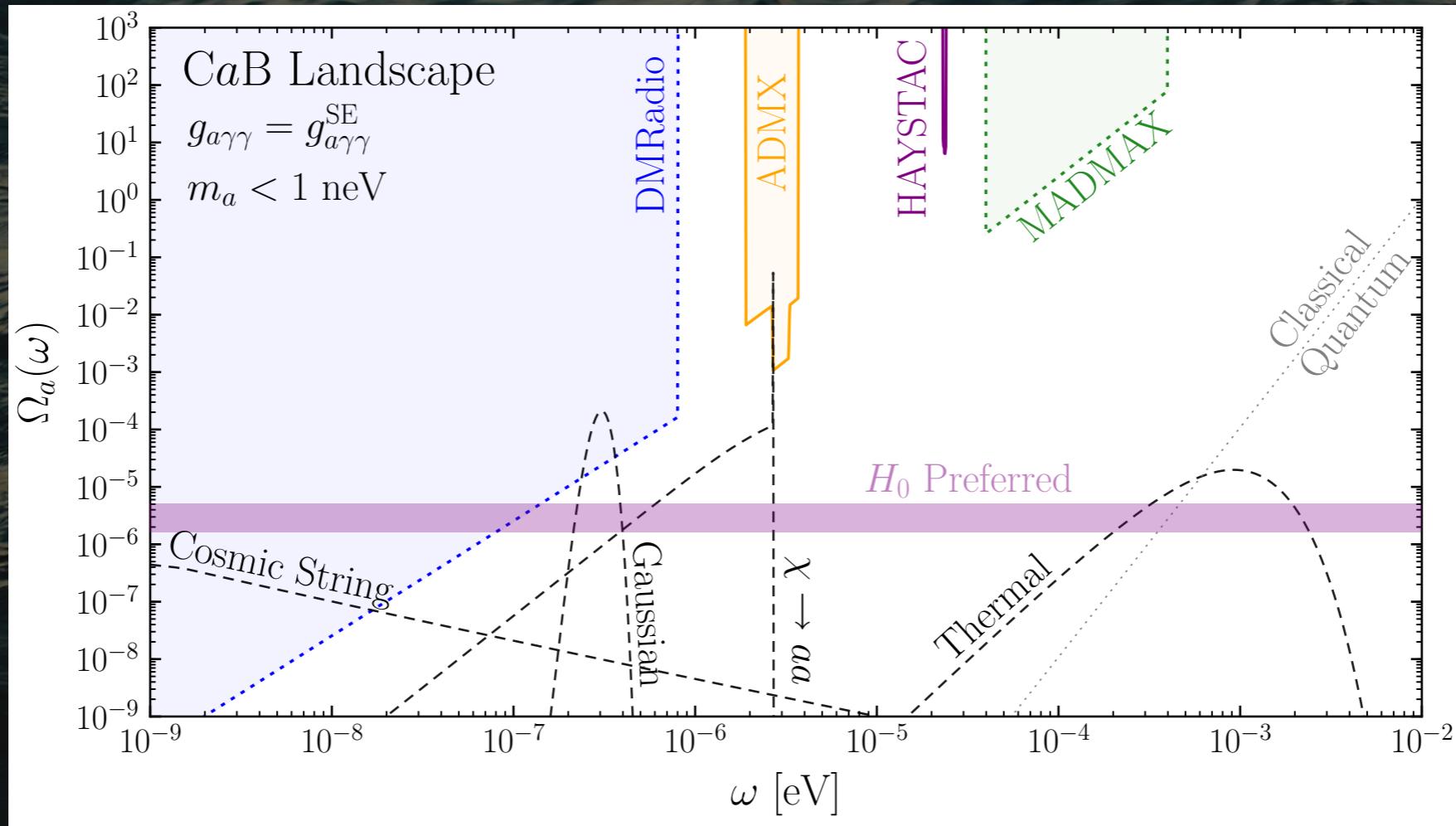
# Future Directions



For another late time production mechanism see [Eby+ 2106.14893]

# Conclusion

Data collected by axion DM instruments is sensitive to a cosmic axion background



# Backup Slides

# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

Introduces corrections to Maxwell's equations

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

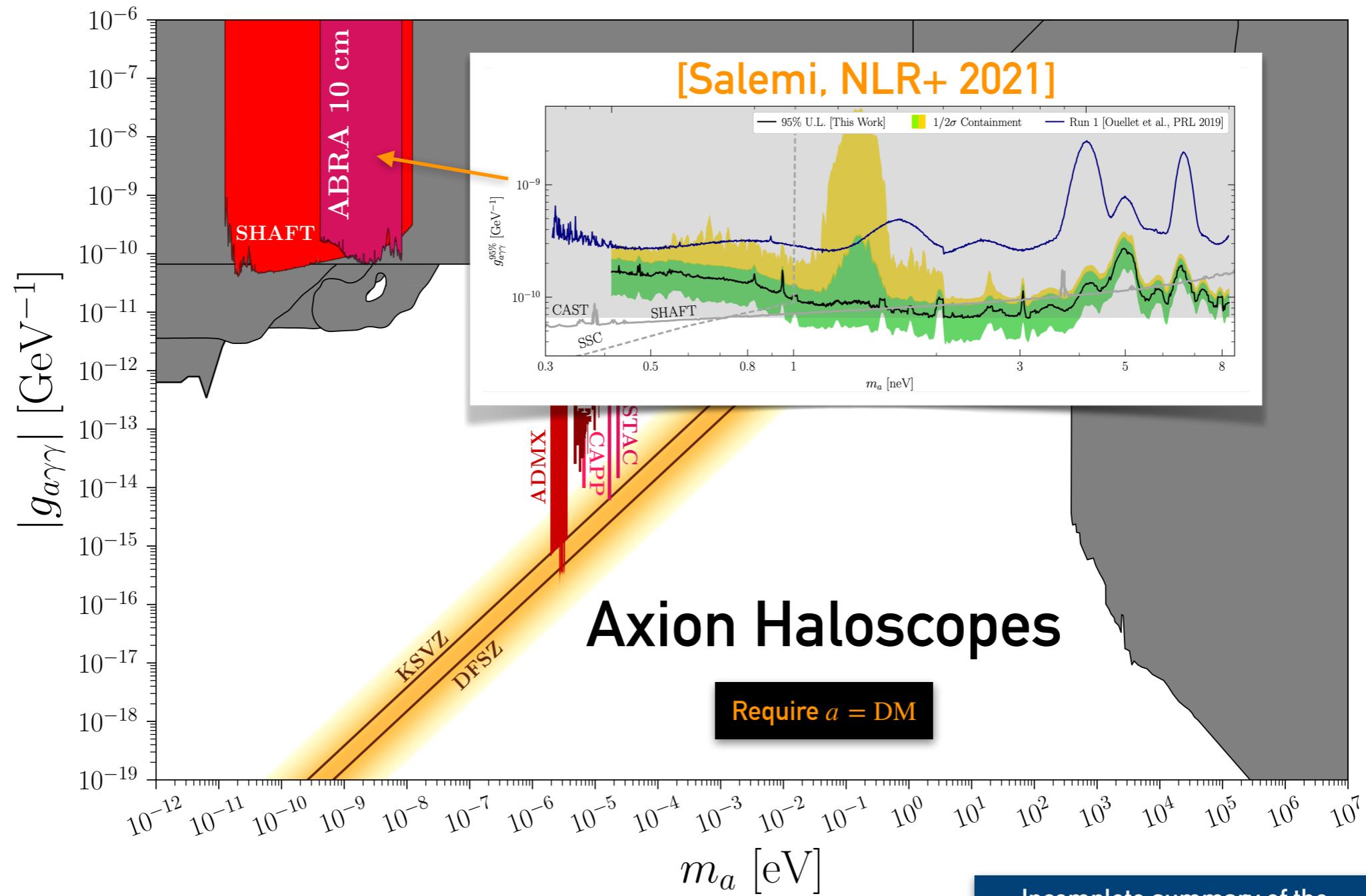
$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} - g_{a\gamma\gamma} (\mathbf{E} \times \nabla a - \mathbf{B} \partial_t a)$$

Suppressed for non-relativistic DM axions

Focus of axion DM searches

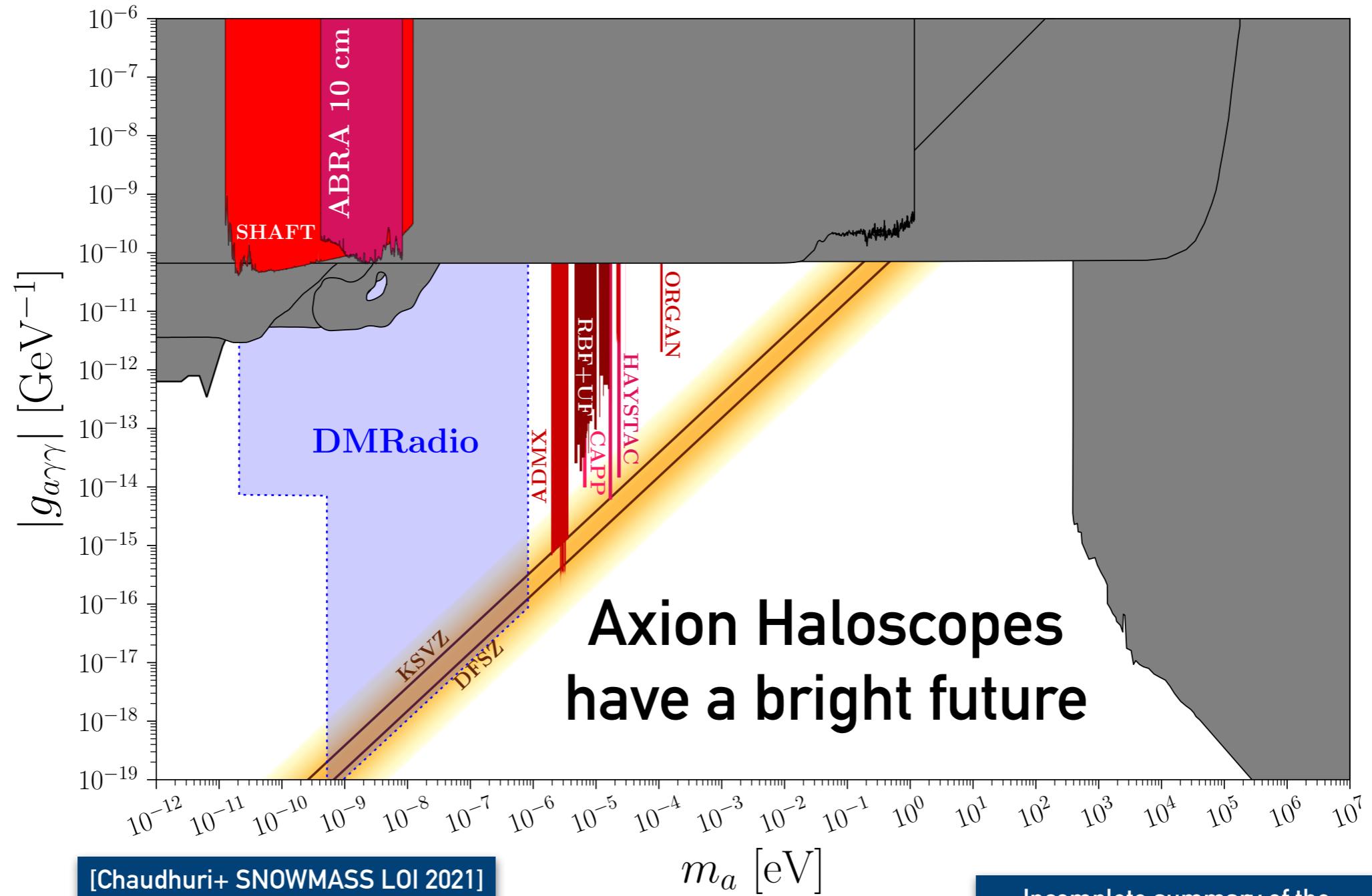
# Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



# Motivation

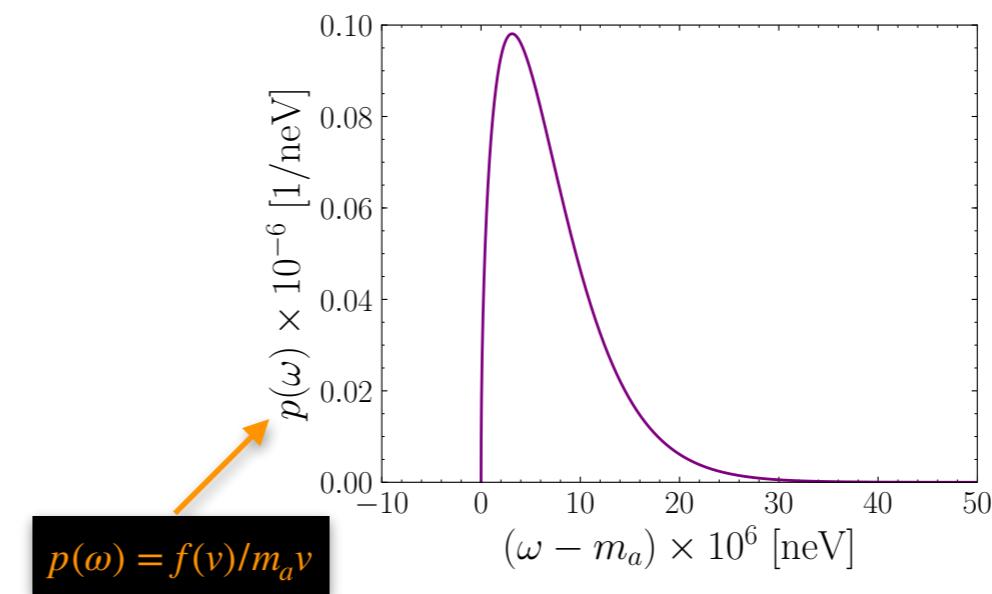
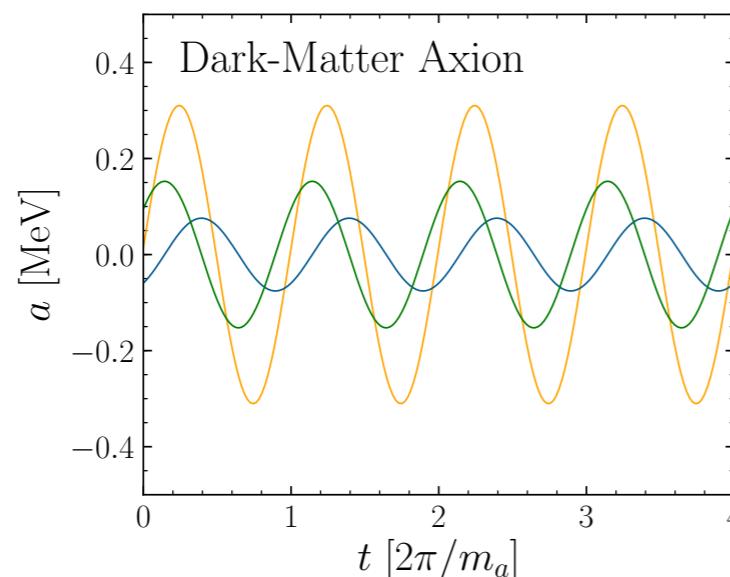
$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



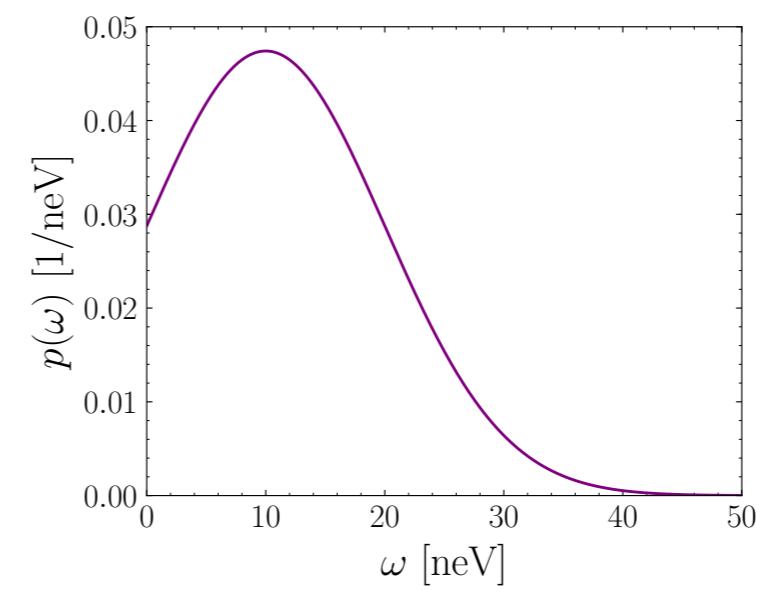
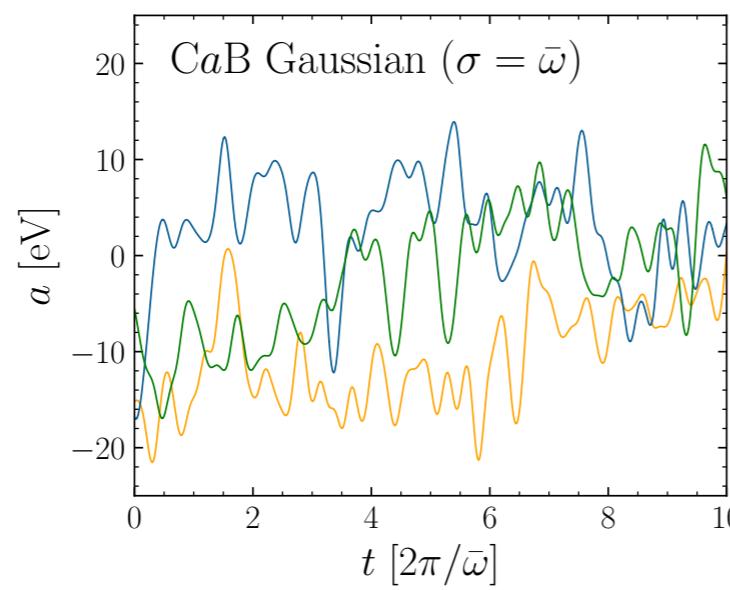
# Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

**Dark Matter**



**CaB**



# Daily Modulation



## Full Equations

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} - g_{a\gamma\gamma} (\mathbf{E} \times \nabla a - \partial_t a \mathbf{B})$$

# Daily Modulation



**Assume only large static  $\mathbf{B}$  field**

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} + g_{a\gamma\gamma} \partial_t a \mathbf{B}$$

# Daily Modulation



Assume only large static  $\mathbf{B}$  field

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0 \qquad \textit{Effective Charge}$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} + g_{a\gamma\gamma} \partial_t a \mathbf{B}$$

*Effective Current*

# Daily Modulation



Sensitive to the incident direction

$$\mathbf{B} \cdot \nabla a = a(t) \mathbf{k} \cdot \mathbf{B}$$



# Daily Modulation



Power deposited sensitive to  $\alpha$

$$P_a^{\text{CaB}} = \frac{\pi}{8} \sin^4 \alpha g_{a\gamma\gamma}^2 Q_a B_0^2 V C \frac{\rho_a}{\bar{\omega}}$$

Daily modulation  
in the signal!

# Bose Enhancement

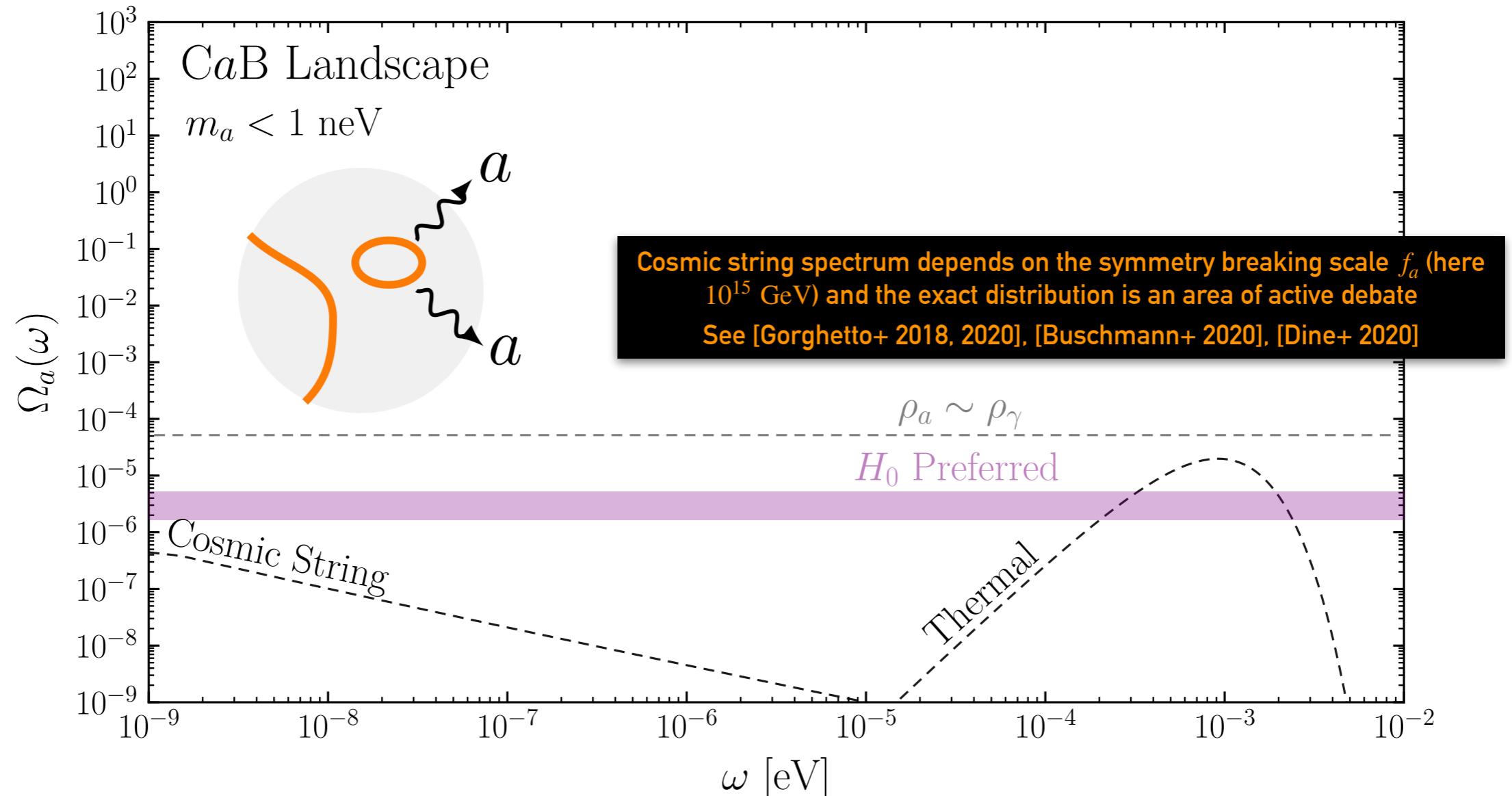


Relevant when  $f_a \gg 1$

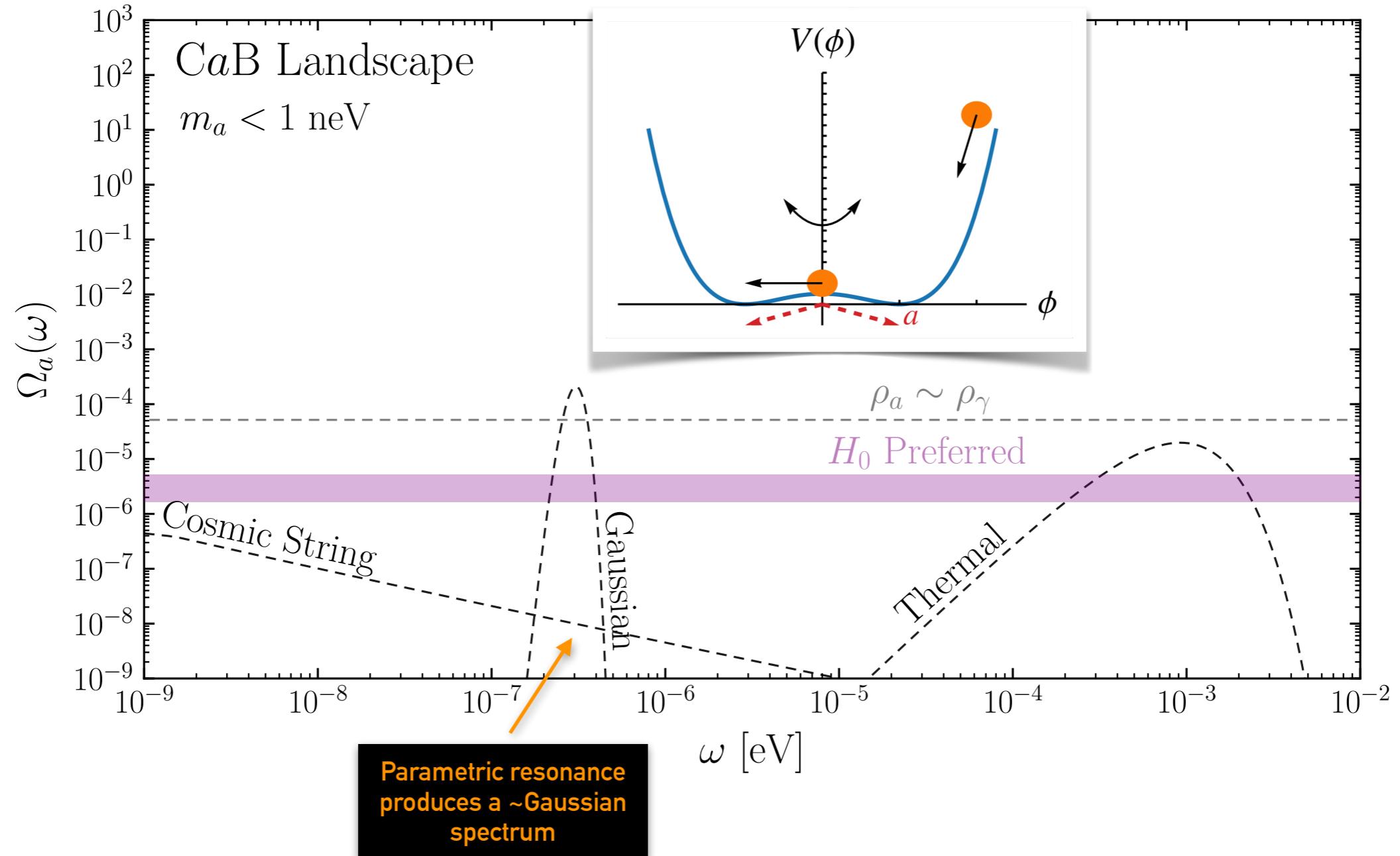
$$f_a = \frac{2\pi^2}{\omega^3} \frac{d\rho_a}{d\omega} \simeq 4 \times 10^{10} \left( \frac{Q_a}{1} \right) \left( \frac{\rho_a}{\rho_\gamma} \right) \left( \frac{\bar{\omega}}{1 \text{ } \mu\text{eV}} \right)^{-4}$$

Large over the entire range we consider

# Landscape



# Landscape



# Parametric Resonance

$$V(\Phi) = \lambda^2 \left( |\Phi|^2 - f_a^2/2 \right)^2$$

Oscillations when  
 $m_\chi^{\text{eff}}(\chi_i) \simeq \lambda \chi_i \sim H$

Typical energy:

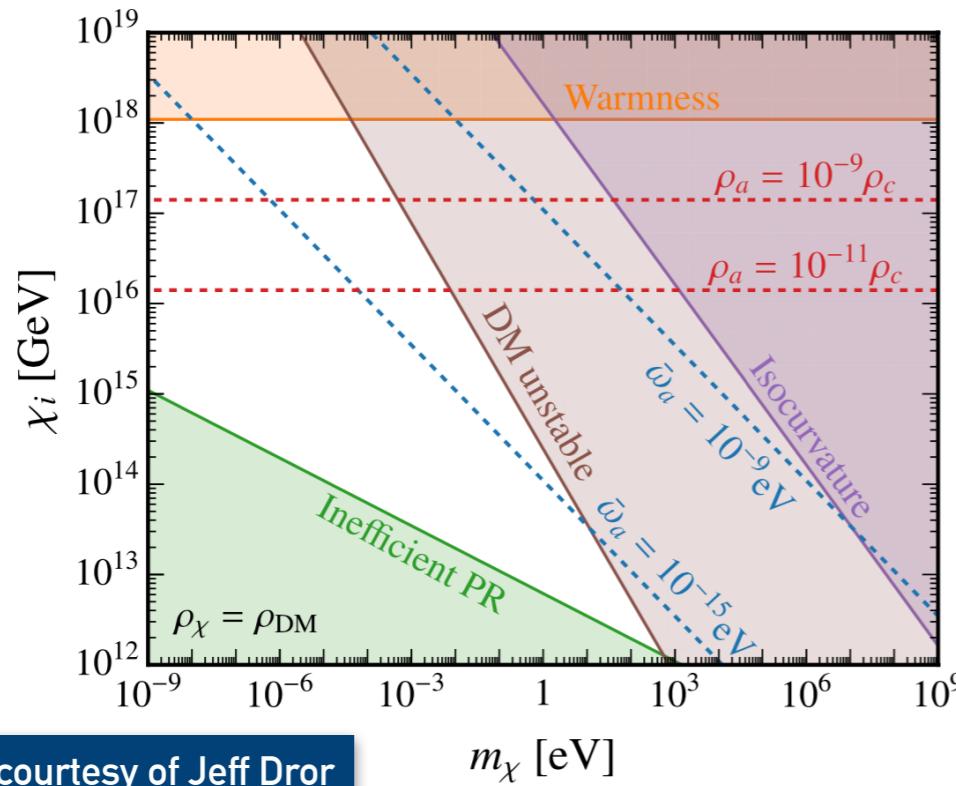
$$\bar{\omega}_a \sim m_\chi^{\text{eff}}(\chi_i) \left( \frac{s(T_0)}{s(T_{\text{osc}})} \right)^{1/3} \sim 10^{-15} \text{ eV} \left( \frac{m_\chi^{\text{eff}}(\chi_i)}{\text{MeV}} \right)^{1/2}$$

Energy density:

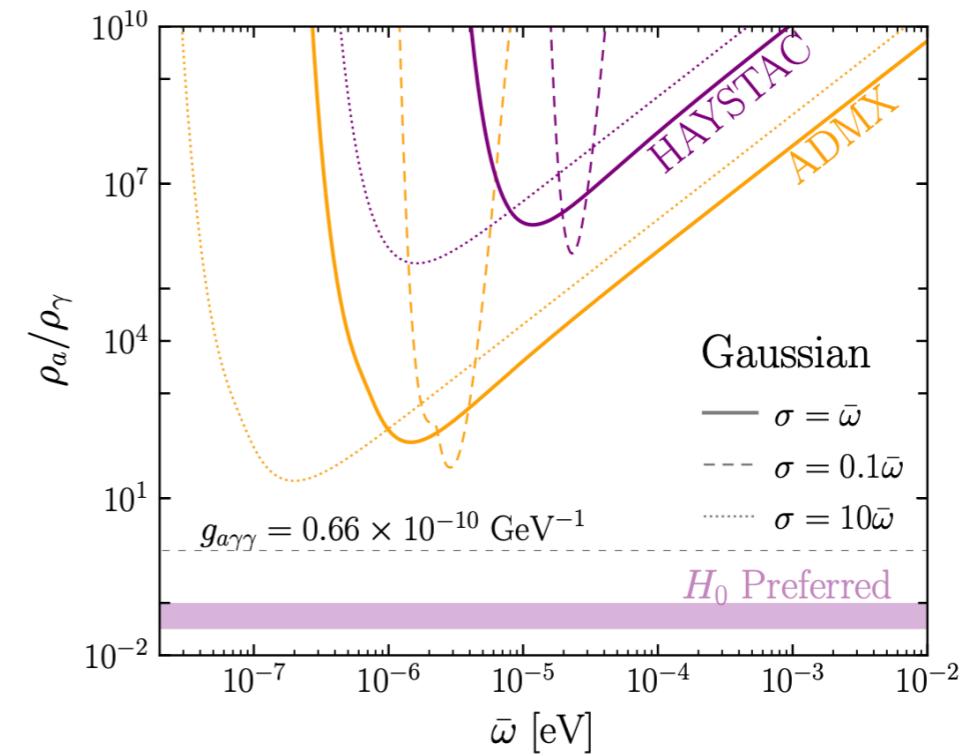
$$\Omega_a \sim 3 \times 10^{-7} \left( \frac{\chi_i}{M_{\text{Pl}}} \right)^2$$

detectable?

**Assume  $\chi$  dark matter**



Slide courtesy of Jeff Dror

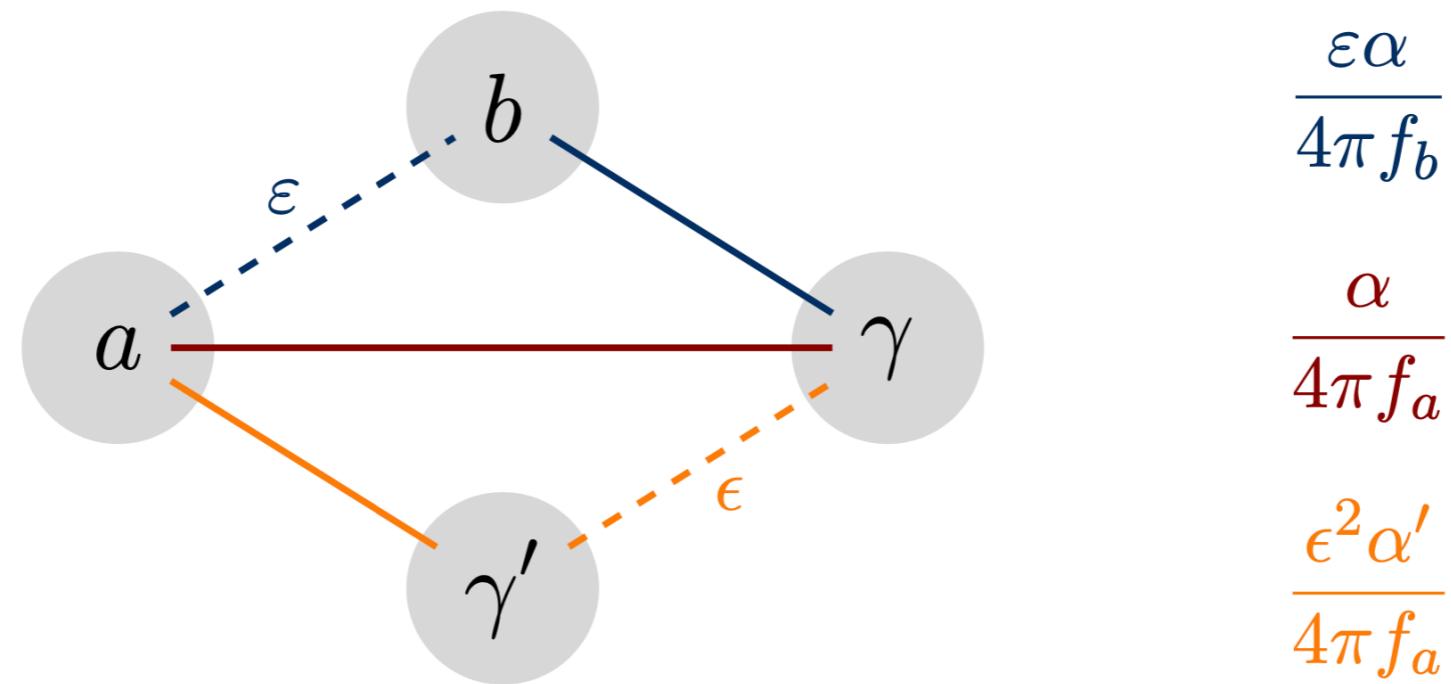


# Dark Matter Decaying to Axions

example  
model

$$V(\Phi) = \lambda^2 \left( |\Phi|^2 - f_a^2/2 \right)^2 \quad \Phi = (\chi + f_a) e^{ia/f_a}$$

$$\frac{\Gamma_{\varphi \rightarrow aa}}{H_0} \simeq \left( \frac{m_\varphi}{10 \text{ } \mu\text{eV}} \right)^3 \left( \frac{100 \text{ MeV}}{f_a} \right)^2 \rightarrow \text{smiley face emoji}$$



Slide courtesy of Jeff Dror